

A theoretical approach to the study of weak interactions in chemistry, biology and materials science

Jorge Echeverría
Inorganic and Organic Chemistry Department
University of Barcelona (Spain)



“BIO-COMP-CHEM” Training School – September 2018 – Bansko (Bulgaria)

NONCOVALENT INTERACTIONS

Noncovalent interactions (NCIs) do not involve the sharing of electrons, but rather involve electrostatics, charge transfer, vdW forces between molecules...

NONCOVALENT INTERACTIONS

Key role in many chemical and biological processes

- Biomolecular function and activity
- Molecular reactivity
- Bulk properties of gases
- Crystal structure
- Macroscopic properties of condensed phases
- Nonlinear optical response of solid state polymers
- Reaction dynamics in liquids
- Solvation phenomena
- Surface and electrode chemistry
- Tribology and adherence of materials

NONCOVALENT INTERACTIONS

Electrostatics

Strength in kcal/mol

- Ionic (NaCl) 250 – 4000
- Hydrogen bonding (H_2O) 5 – 40
- Hole interactions (halogen, chalcogen, etc.) 1 – 20

Van der Waals

- Debye forces (permanent- induced dipoles) 1 – 10
- London dispersion (alkanes)

π -effects

- π/π stacking (graphite) 1 – 20
- Cation and anion- π ($\text{Cl}^- - \text{C}_6\text{F}_6$)

Computational tools

Electronic structure calculations

Post-HF	CCSD(T)	“Gold Standard”	
	MP2	Good but... tends to overestimate NCIs	
DFT	Periodic	vdW description of surface	
	Gas phase	B3LYP-D3	for dihydrogen bonds
		LC- ω PBE-D3BJ	for metallophilic interactions
		M06-2X	for halogen bonding

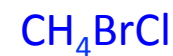
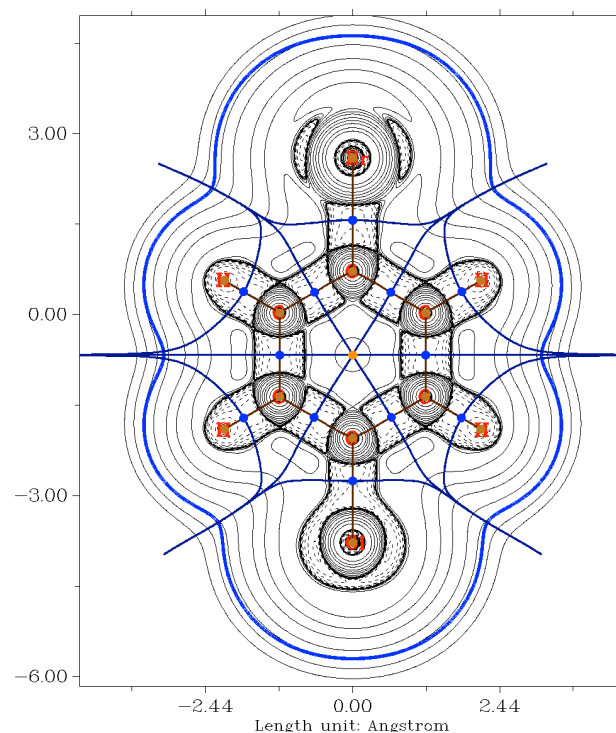
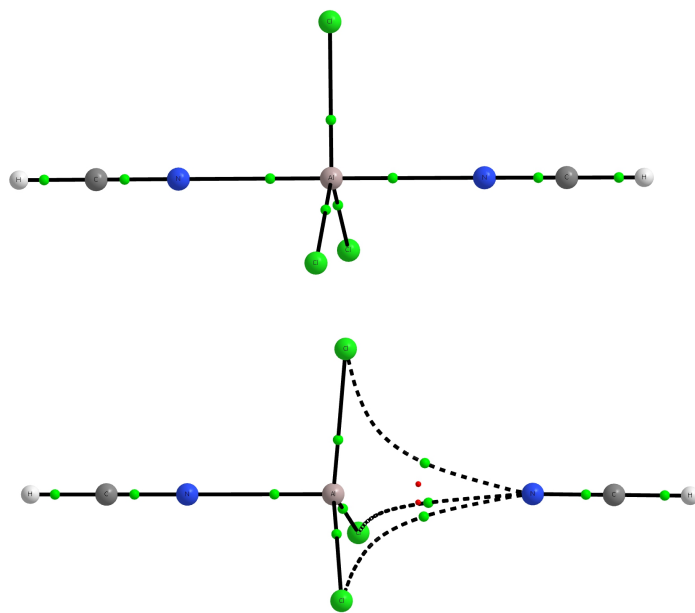
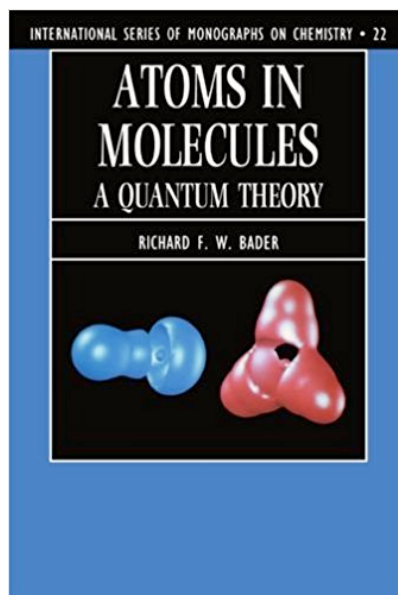
Basis sets Triple- ξ mandatory, polarization and diffuse recommended

Benchmarking is usually the safest option!

Computational tools

Quantum Theory of Atoms in Molecules – QTAIM ([AIMAll](#))

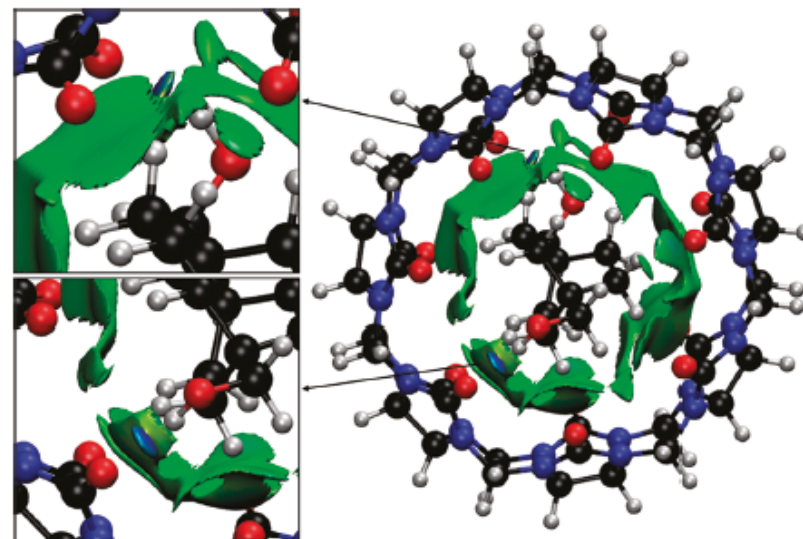
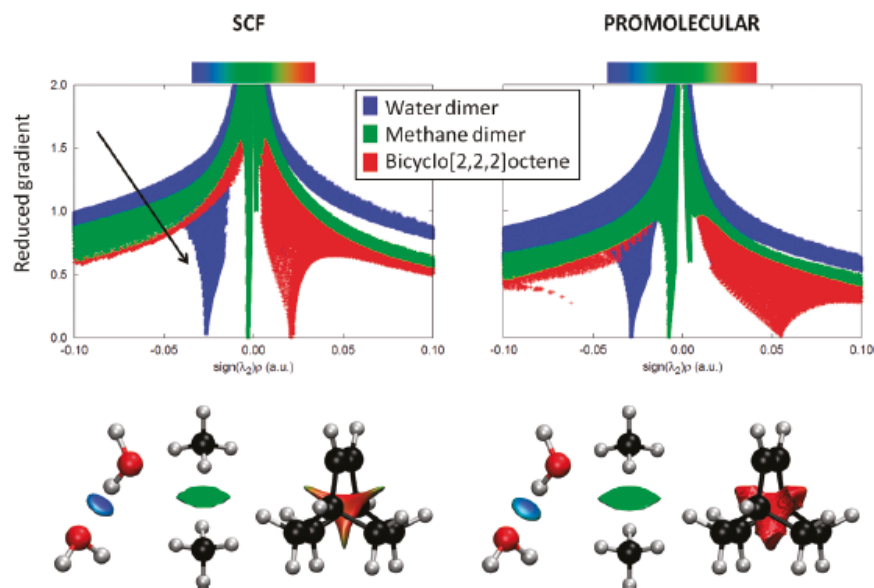
Analyzes the topology of the electron density



R. Bader, *Atoms in Molecules: A Quantum Theory*. USA: Oxford University Press. (1994)

Computational tools

NCI index calculations (NCIPLOT)

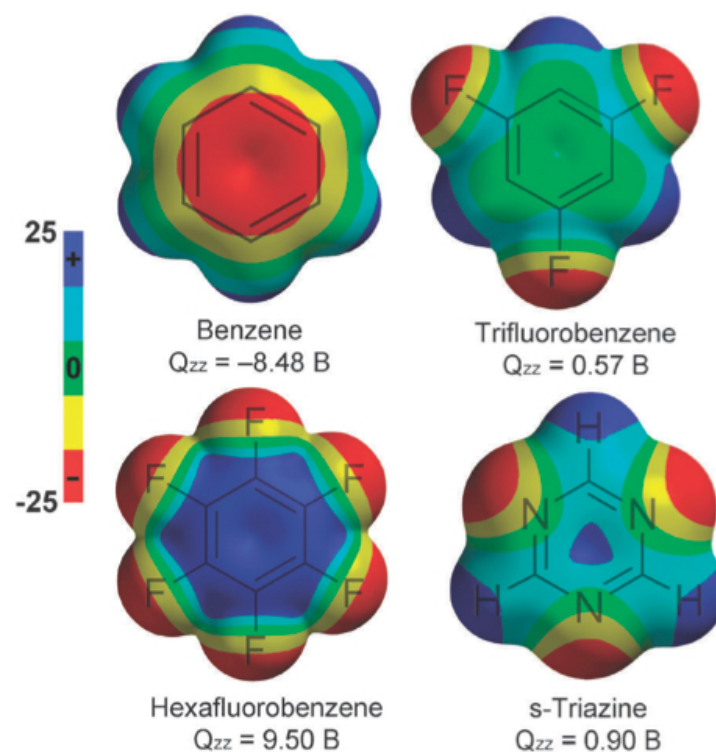


Identification of intermolecular interactions
based on the electron density and its derivatives

Computational tools

Molecular Electrostatic Potential– MEP (GaussView)

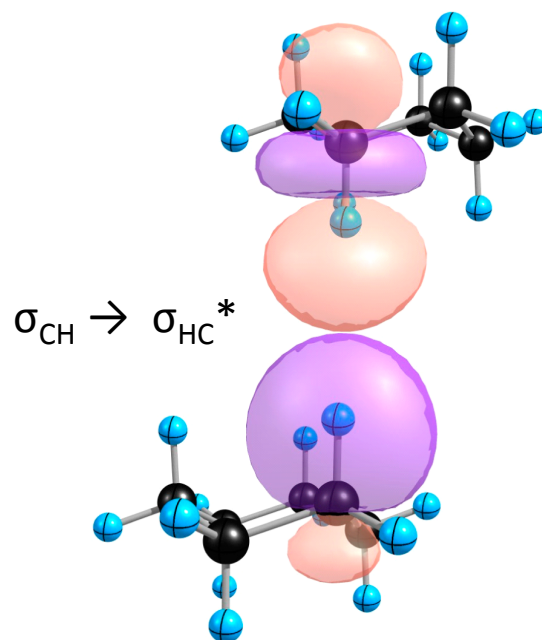
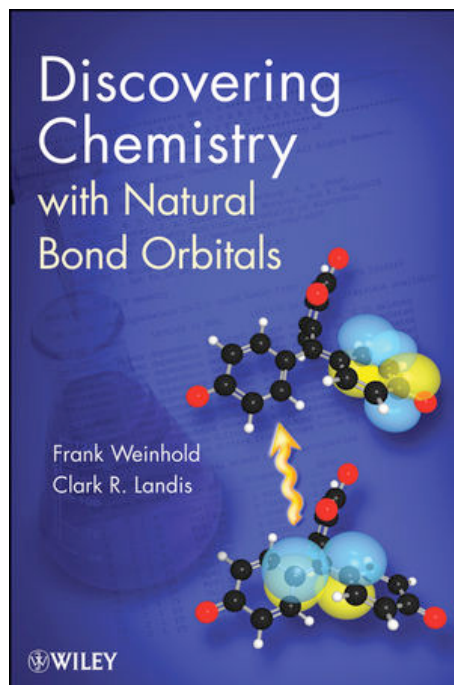
- Assesses the molecules reactivity towards positively or negatively charged reactants
- Mapped onto a surface reflecting the molecules boundaries



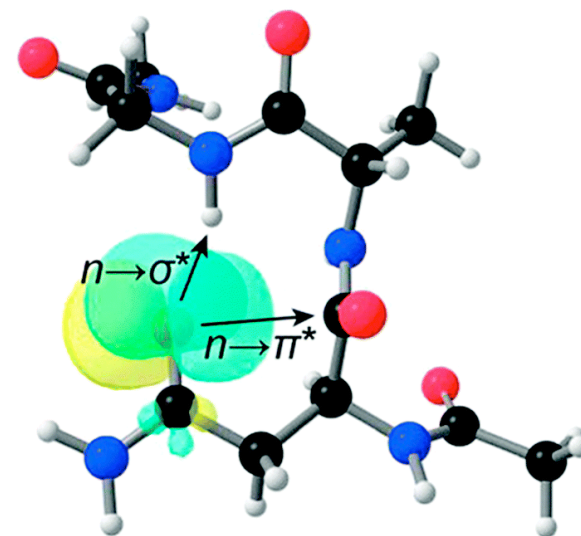
Computational tools

Natural Bond Orbitals – NBO Analysis ([NBO6](#), [Gaussian](#))

Atomic Orbital $\rightarrow$ NAO $\rightarrow$ NHO $\rightarrow$ **NBO** $\rightarrow$ NLMO $\rightarrow$ Molecular orbital



Intermolecular



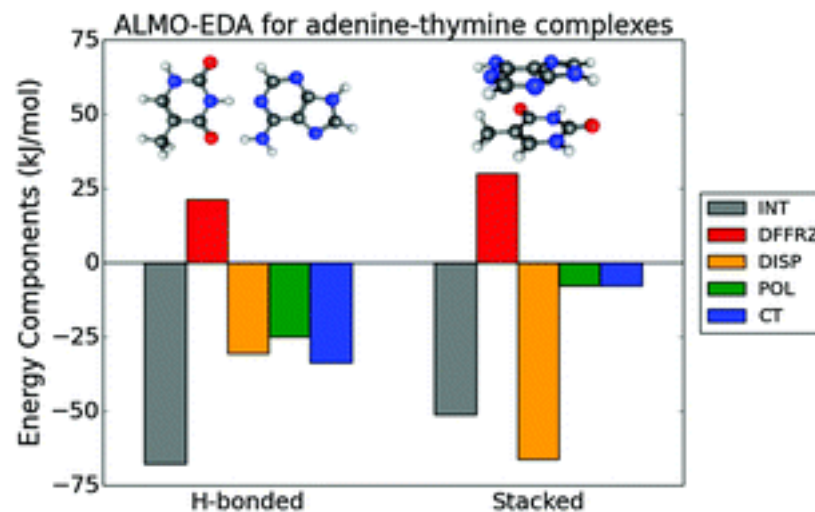
Intramolecular

Computational tools

Energy Decomposition Analysis – EDA (Q-Chem, GAMESS, ADF, etc.)

- There are in fact many EDAs... ALMO-EDA, EDA-NOCV, SAPT(DFT)...
- Decomposes total interaction energy in a supermolecule into several energetic terms that are chemically meaningful

$$\Delta E_{\text{int}} = \Delta E_{\text{Pauli}} + \Delta E_{\text{elect}} + \Delta E_{\text{disp}} + \Delta E_{\text{pol}} + \Delta E_{\text{CT}}$$

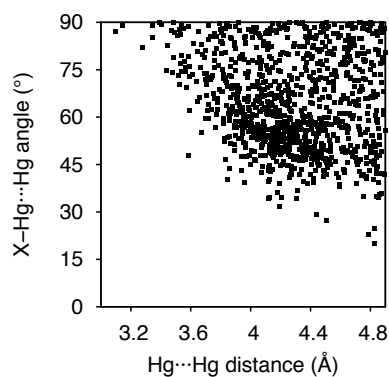


Computational tools

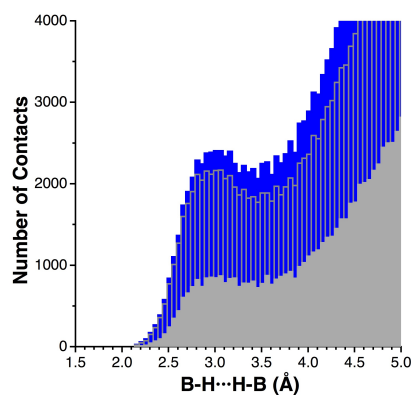
Structural database mining

Access to millions of crystal structures: CSD, PDB, ICSD, Mogadoc...

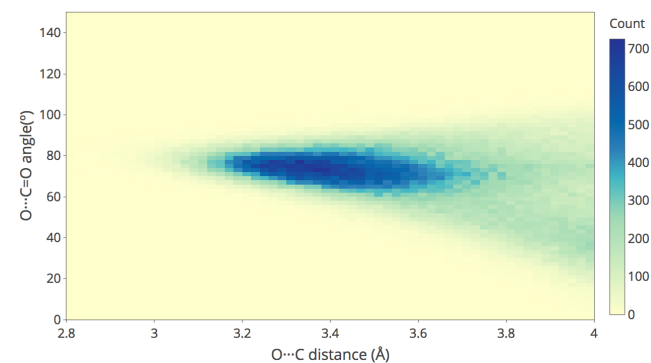
Angular dependence



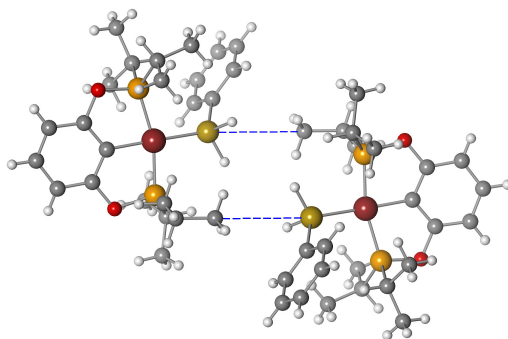
Occurrence



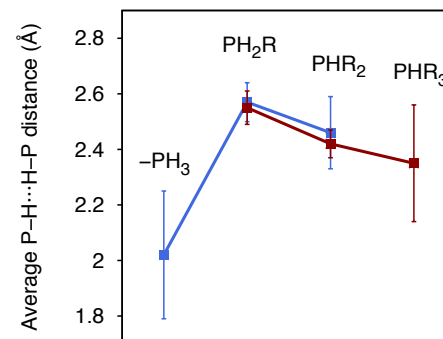
2D histogram (Heat maps)



Specific examples



General trends



The Cambridge Structural Database

What is the CSD?

The CSD is a molecular repository operated by the CCDC



Initially (1965) part of the University of Cambridge ,
today an independent non-profit organisation.

The Cambridge Structural Database

What's in the CSD?

The CSD contains X-ray and neutron diffraction analyses of carbon-containing molecules up to 1000 atoms including:

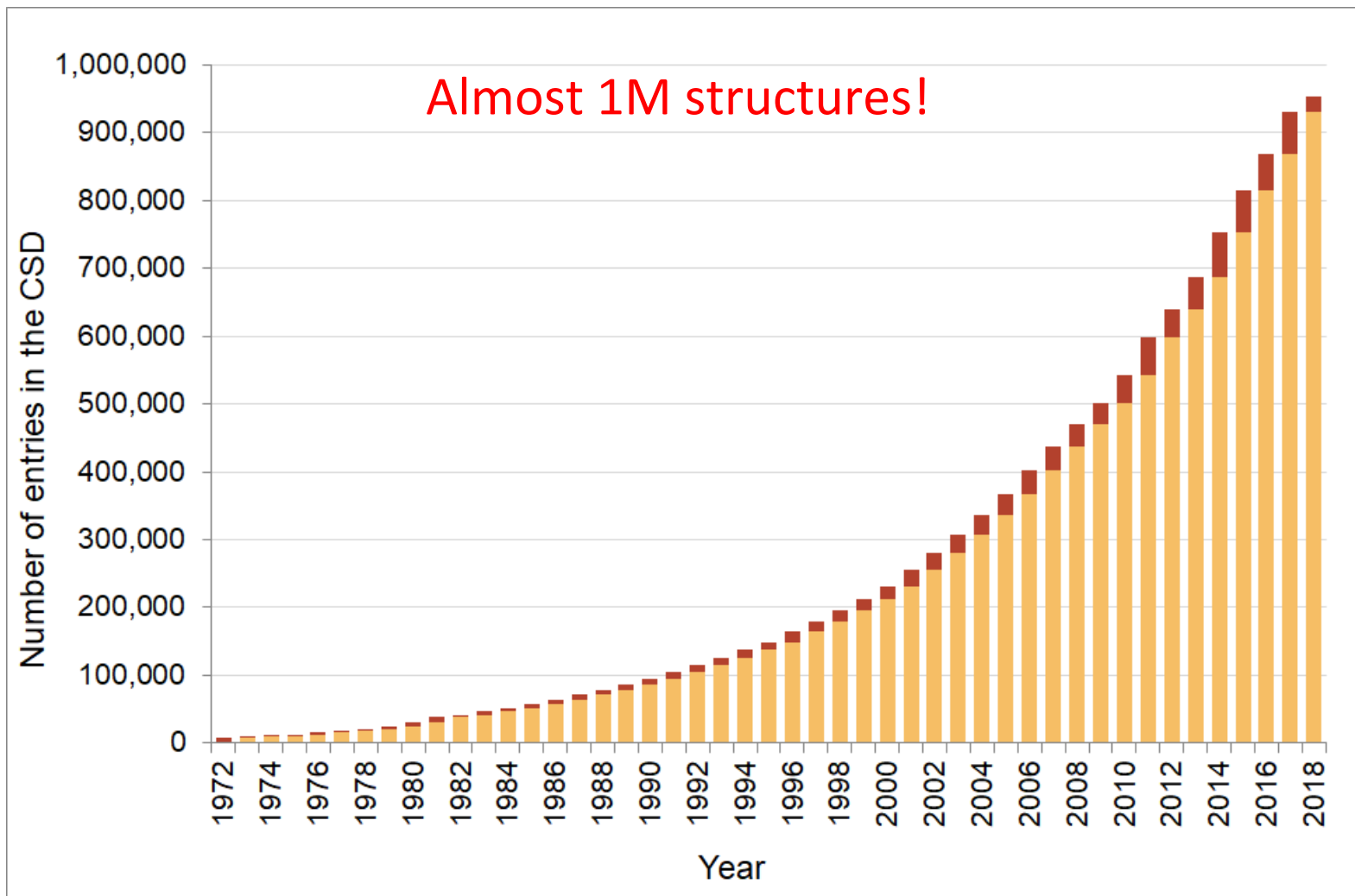
- Organics
- Compounds of the main group elements
- Organometallics
- Metal complexes

The CSD covers peptides of up to 24 residues;

higher oligomers are covered by the Protein Data Bank ([see Dr. Cirera's tutorial](#)).

The Cambridge Structural Database

How big is the CSD?



The Cambridge Structural Database

CSD Refcodes (Entry identifiers)

- Six letters, e.g. ABACOF
- Two digits additional structure determinations, e.g. ABACOF03

For each entry (when possible):

- Bibliographic info. (Author, journal, DOI ...)
- Chemical info. (formula, diagram ...)
- Crystallographic info. (space group, R-factor ...)
- Extra text info. (disorder, polymorphism ...)

The Cambridge Structural Database

A typical CSD entry

Refcode: ACACCS

Author(s): F.A.Cotton, C.E.Rice, G.W.Rice

Journal: Inorg.Chim.Acta

Volume: 24

Page: 231

Year: 1977

Formula: C₁₀ H₁₄ Cr₁ O₄

Name: bis(2,4-Pentanedionato) chromium

Spacegroup

Name: P2₁/n

Number: 14

Cell Parameters

a: 11.445

b: 4.748

c: 10.325

alpha: 90.00

beta: 91.60

gamma: 90.00

Volume: 560.851

Reduced Cell Parameters

a: 4.748

b: 10.325

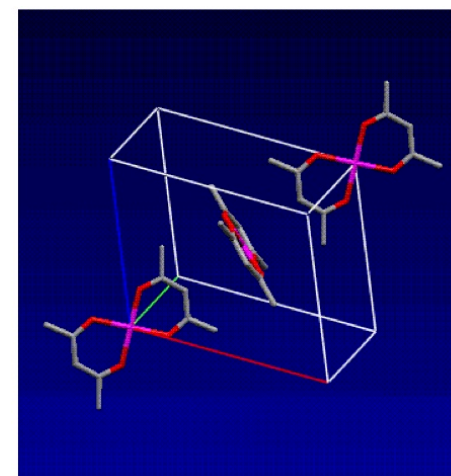
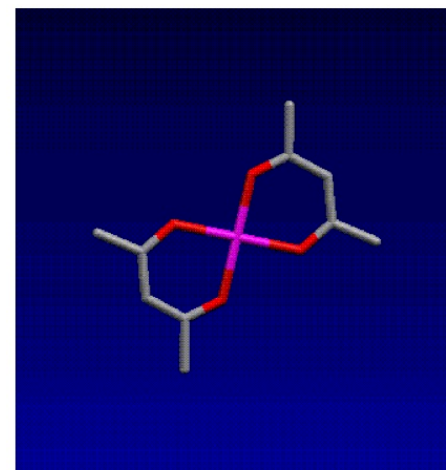
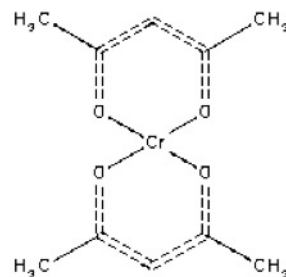
c: 11.445

alpha: 91.60

beta: 90.00

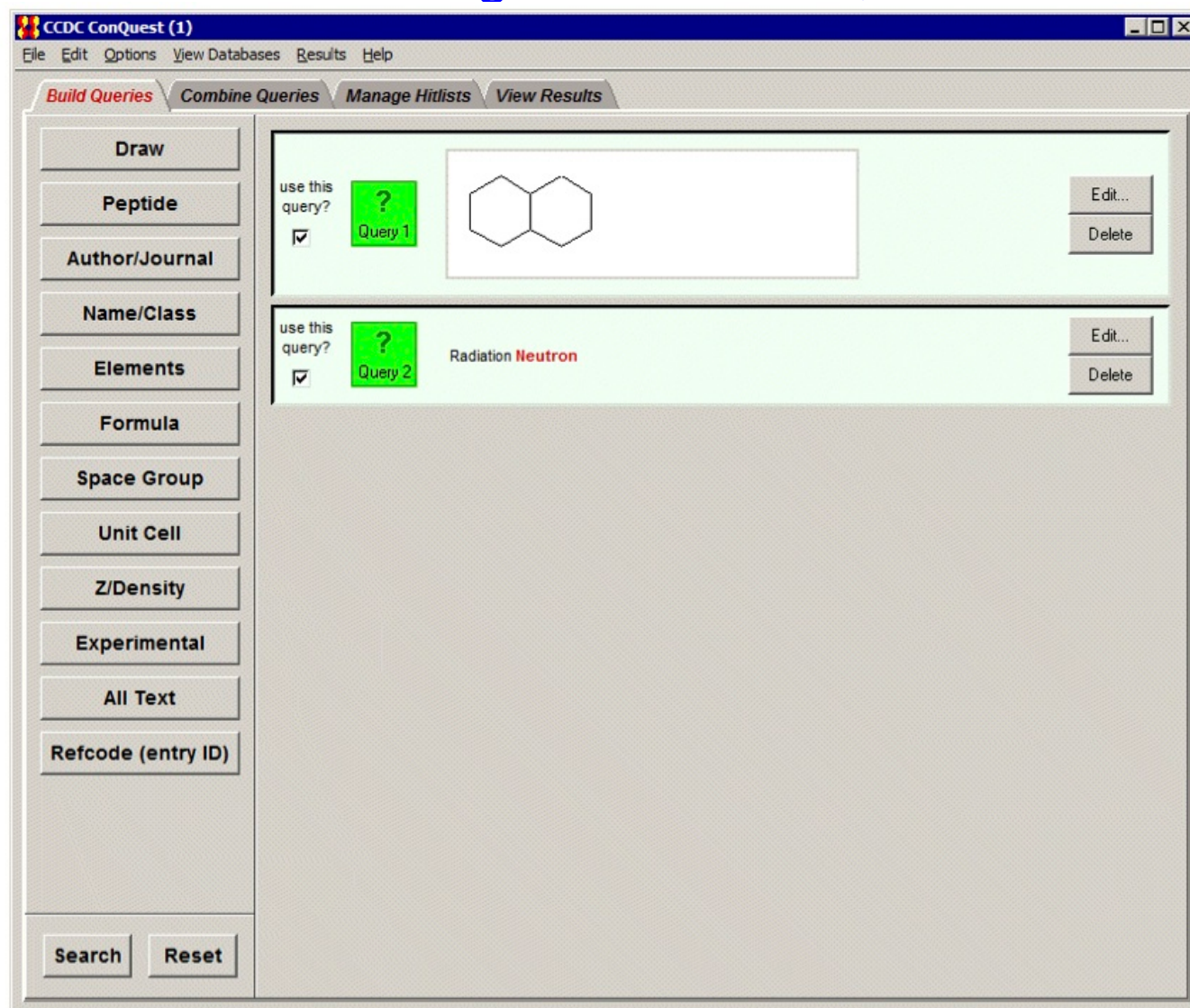
gamma: 90.00

Volume: 560.848



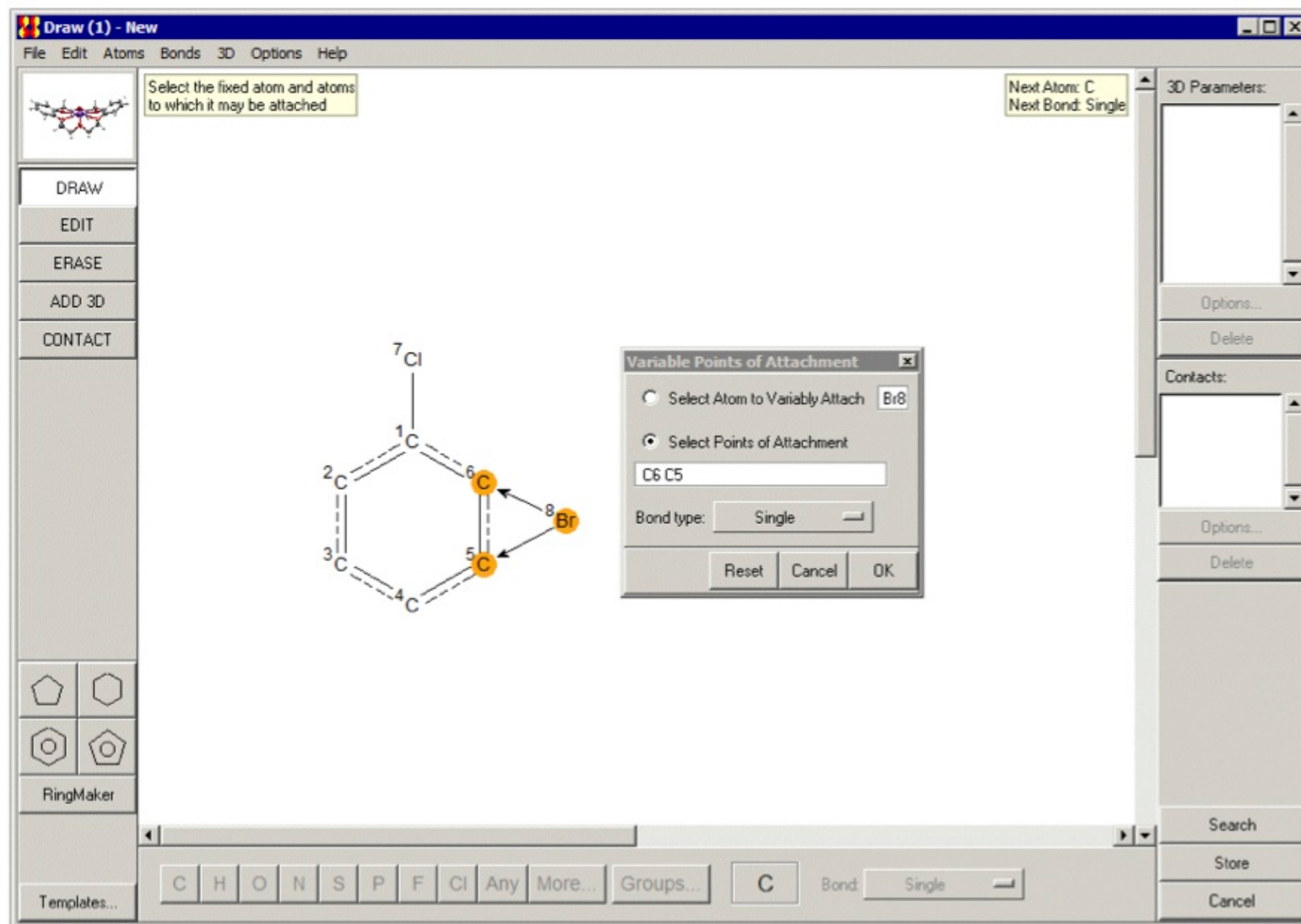
The Cambridge Structural Database

Searching the CSD: ConQuest



The Cambridge Structural Database

Searching the CSD: ConQuest



The Cambridge Structural Database

Combine queries

CCDC ConQuest (1)

File Edit Options View Databases Results Help

Build Queries **Combine Queries** Manage Hitlists View Results

Drag Query Icons into Boxes

Find entries that:

must have (boolean AND)

Query 4

must not have (NOT)

Query 3

must have at least one of (OR)

Query 1 Query 2

Search Reset

Query 1
Elements **Mg**
Search on: **Sum of molecules**
Allow other elements: **Yes**
Edit...
Delete

Query 2

Edit...
Delete

Query 3
Space Group **P21/c (and equivalent space groups)**
Edit...
Delete

Query 4
Temperature **< 273 K**
Edit...
Delete

Query 5
Z = 4
Edit...
Delete

The Cambridge Structural Database

Start searches

The image shows a screenshot of the 'Search Setup' dialog box from the Cambridge Structural Database software. The dialog has a title bar with the Cambridge logo and the text 'Search Setup'. It is divided into several sections. At the top, there is a 'Search Name' field containing 'search7'. Below this, under 'Available Databases:', there is a list box with one entry: 'CSD version 5.34 (November 2012)', which is checked. Below the list box, there is a text box explaining that users can search the complete database or a subset of hits from a previous search, with 'Select Subset' and 'Clear Subset' buttons. Below that, a text box states 'Single query being used. Search will find structures: where this query is true:', followed by a green button labeled 'Query 7'. On the right side, there are two tabs: 'Filters' (selected) and 'Advanced Options'. Under the 'Filters' tab, there are several checkboxes: '3D coordinates determined' (unchecked), 'R factor' (unchecked) with three radio button options for thresholds: '<= 0.05' (selected), '<= 0.075' (unchecked), and '<= 0.1' (unchecked). Other unchecked filters include 'Not disordered', 'No errors', 'Not polymeric', 'No ions', and 'No powder structures'. At the bottom of the 'Filters' tab, there is a group box with 'Only' (unchecked) and two radio button options: 'Organics' (selected) and 'Organometallic' (unchecked). At the bottom of the dialog, there are three buttons: 'Start Search', 'Cancel', and 'Reset'.

Search Setup

Search Name: search7

Available Databases:

- ☒ CSD version 5.34 (November 2012)

You can search complete database(s) or a subset (e.g., hits found in a previous search)

Select Subset Clear Subset

Single query being used. Search will find structures:
where this query is true:
Query 7

Filters **Advanced Options**

- ☐ 3D coordinates determined
- ☐ R factor
 - ☒ <= 0.05
 - ☐ <= 0.075
 - ☐ <= 0.1
- ☐ Not disordered
- ☐ No errors
- ☐ Not polymeric
- ☐ No ions
- ☐ No powder structures
- ☐ Only
 - ☒ Organics
 - ☐ Organometallic

Start Search Cancel Reset

The Cambridge Structural Database

Manage hitlists

CCDC ConQuest (1) : search2 [Search]

File Edit Options View Databases Results Help

Build Queries Combine Queries **Manage Hitlists** View Results

Combine Hitlists

Combination Name: combination2

List A: search1 List B: search2

Include deselected entries in:

☐ List A ☐ List B

Generate a List of Entries:

☒ common to List A and List B

☐ in either List A or List B

☐ in List A but not in List B

OK

Hitlist Overview

combination1 (2202 Entries) ☐ Full overview ☐ Single line

search1
and
search2

Name	Hits	Type
combination1	2202	Combination
search1	2202	Search
search2	207174	Search

Delete Rename... Notes... View

The Cambridge Structural Database

View results

CCDC ConQuest (1) : search1 [Search]

File Edit Options View Databases Results Help

Build Queries Combine Queries Manage Hitlists **View Results**

Refcode: ABEKEX CSD version 5.32 (November 2010)

Diagram

Chemical structure diagram of ABEKEX, a complex polycyclic molecule. The structure features a central ring system with two ethyl (Et) groups attached. A sulfur atom (S) is part of a five-membered ring fused to the main structure. The molecule also includes several other fused and linked rings, including a naphthalene-like system at the bottom.

ABEKEX

Analyse Hitlist

- ✓ ABADIR
- ✓ ABAF0Z
- ✓ ABAGAM
- ✓ ABALIZ
- ✓ ABECAL
- ✓ ABEGAP
- ✓ ABEGAP01
- ✓ ABEKEX**
- ✓ ABEKIB
- ✓ ABEKOH
- ✓ ABESAB
- ✓ ABESEF
- ✓ ABESG
- ✓ ABESG01
- ✓ ABIBAO
- ✓ ABIBES
- ✓ ABIGEY
- ✓ ABIGEY01
- ✓ ABIGIB
- ✓ ABIXUE
- ✓ ABIYAL
- ✓ ABOGEE
- ✓ ABOGII
- ✓ ABOPIR
- ✓ ABOOOX
- ✓ ABOTUH
- ✓ ABOVAP
- ✓ ABOVAP01

511 hits

3%

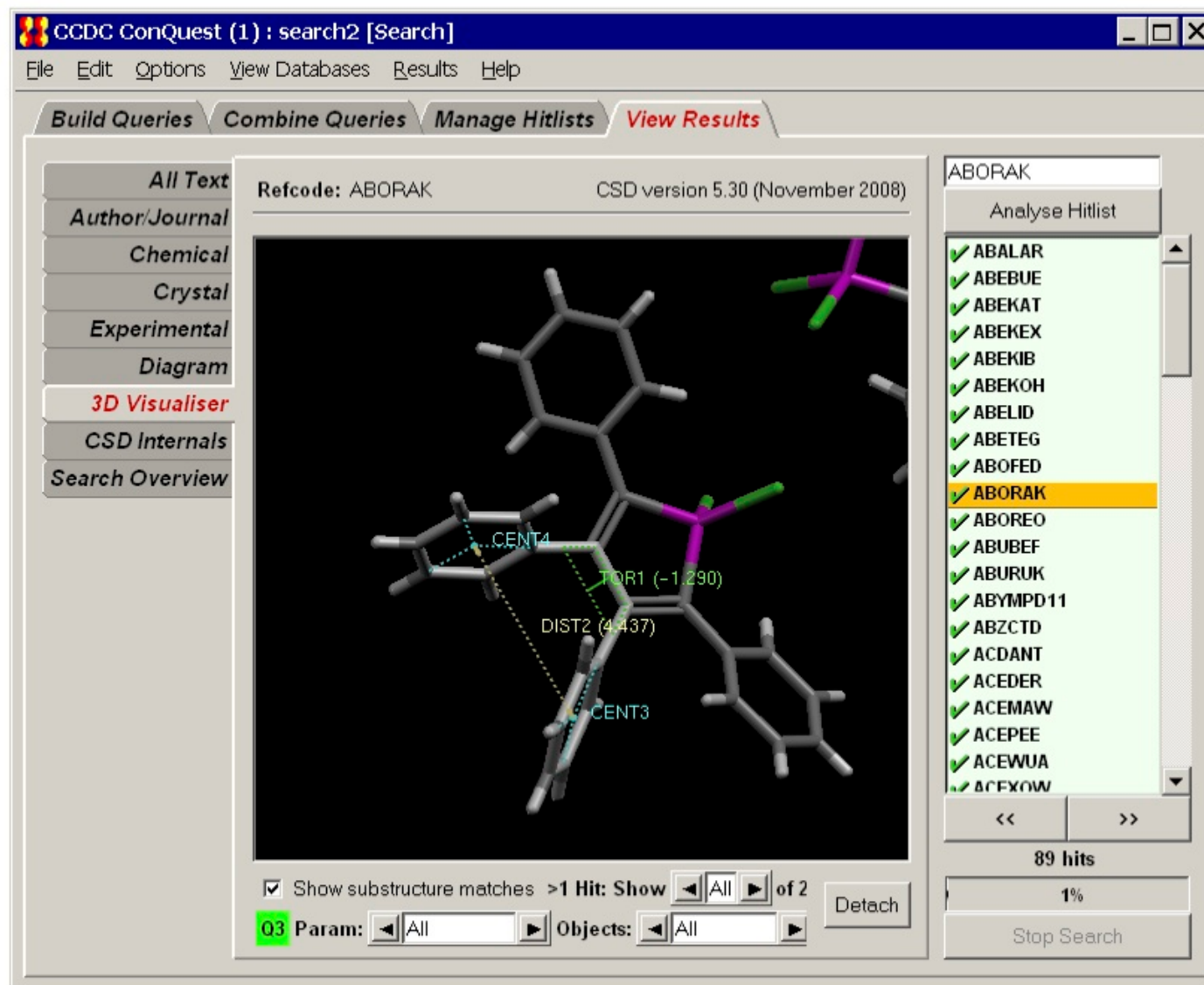
Stop Search

☐ Show terminal carbons

Use as Query... Detach

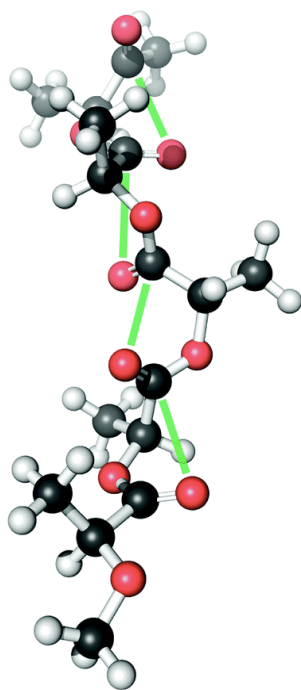
The Cambridge Structural Database

3D visualizer

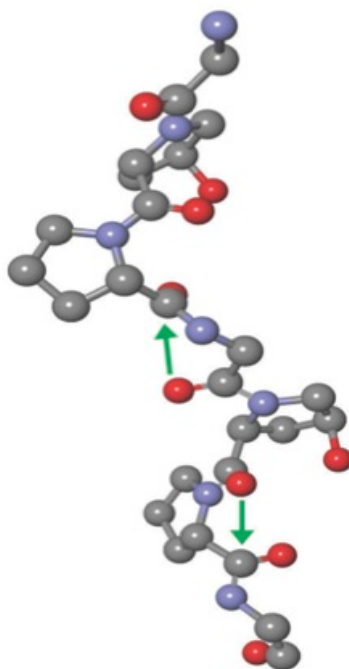


A case study

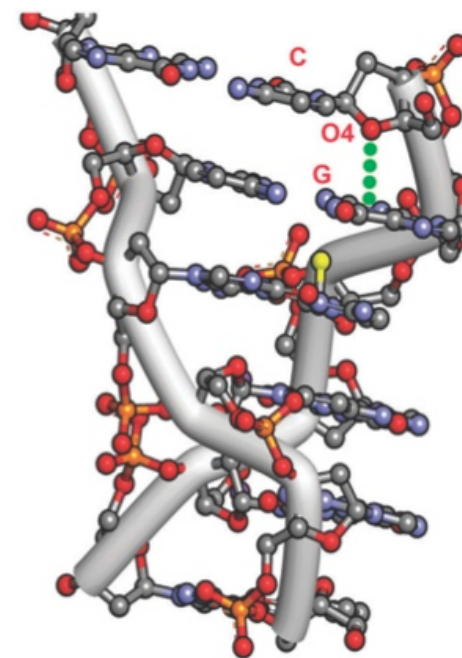
The $n \rightarrow \pi^*$ interaction



Poly-Lactic Acid



Collagen triple-helix



Z-DNA [PDB ID-131D]

The $n \rightarrow \pi^*$ interaction

This is an open access article published under an ACS AuthorChoice License, which permits copying and redistribution of the article or any adaptations for non-commercial purposes.



Article

pubs.acs.org/accounts

ACCOUNTS
of chemical research

The $n \rightarrow \pi^*$ Interaction

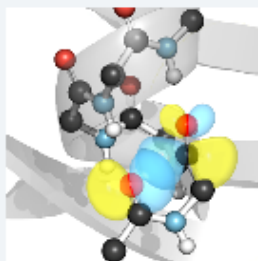
Published as part of the Accounts of Chemical Research special issue "Chemical Biology of Peptides".

Robert W. Newberry[†] and Ronald T. Raines^{*,†,‡}

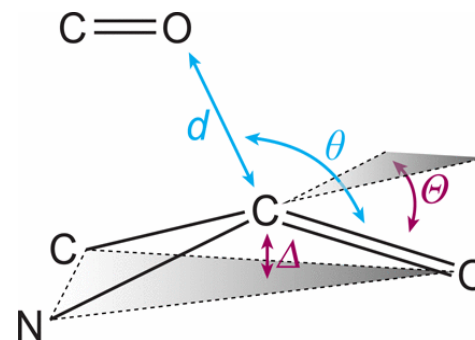
[†]Department of Chemistry, University of Wisconsin–Madison, Madison, Wisconsin 53706, United States

[‡]Department of Biochemistry, University of Wisconsin–Madison, Madison, Wisconsin 53706, United States

CONSPECTUS: The carbonyl group holds a prominent position in chemistry and biology not only because it allows diverse transformations but also because it supports key intermolecular interactions, including hydrogen bonding. More recently, carbonyl groups have been found to interact with a variety of nucleophiles, including other carbonyl groups, in what we have termed an $n \rightarrow \pi^*$ interaction. In an $n \rightarrow \pi^*$ interaction, a nucleophile donates lone-pair (n) electron density into the empty π^* orbital of a nearby carbonyl group. Mixing of these orbitals releases energy, resulting in an attractive interaction. Hints of such interactions were evident in small-molecule crystal structures as early as the 1970s, but not until 2001 was the role of such interactions articulated clearly. These non-covalent interactions were first discovered during investigations into the thermostability of the proline-rich protein collagen, which achieves a robust structure despite a relatively low potential for hydrogen bonding. It was found that by modulating the distance between two carbonyl groups in the peptide backbone, one could alter the conformational preferences of a peptide bond to proline. Specifically, only the trans conformation of a peptide bond to proline allows for an attractive interaction with an adjacent carbonyl group, so when one increases the proximity of the two carbonyl groups, one enhances their interaction and promotes the trans conformation of the peptide bond, which increases the thermostability of collagen.



- Most common $C=O \cdots C=O$



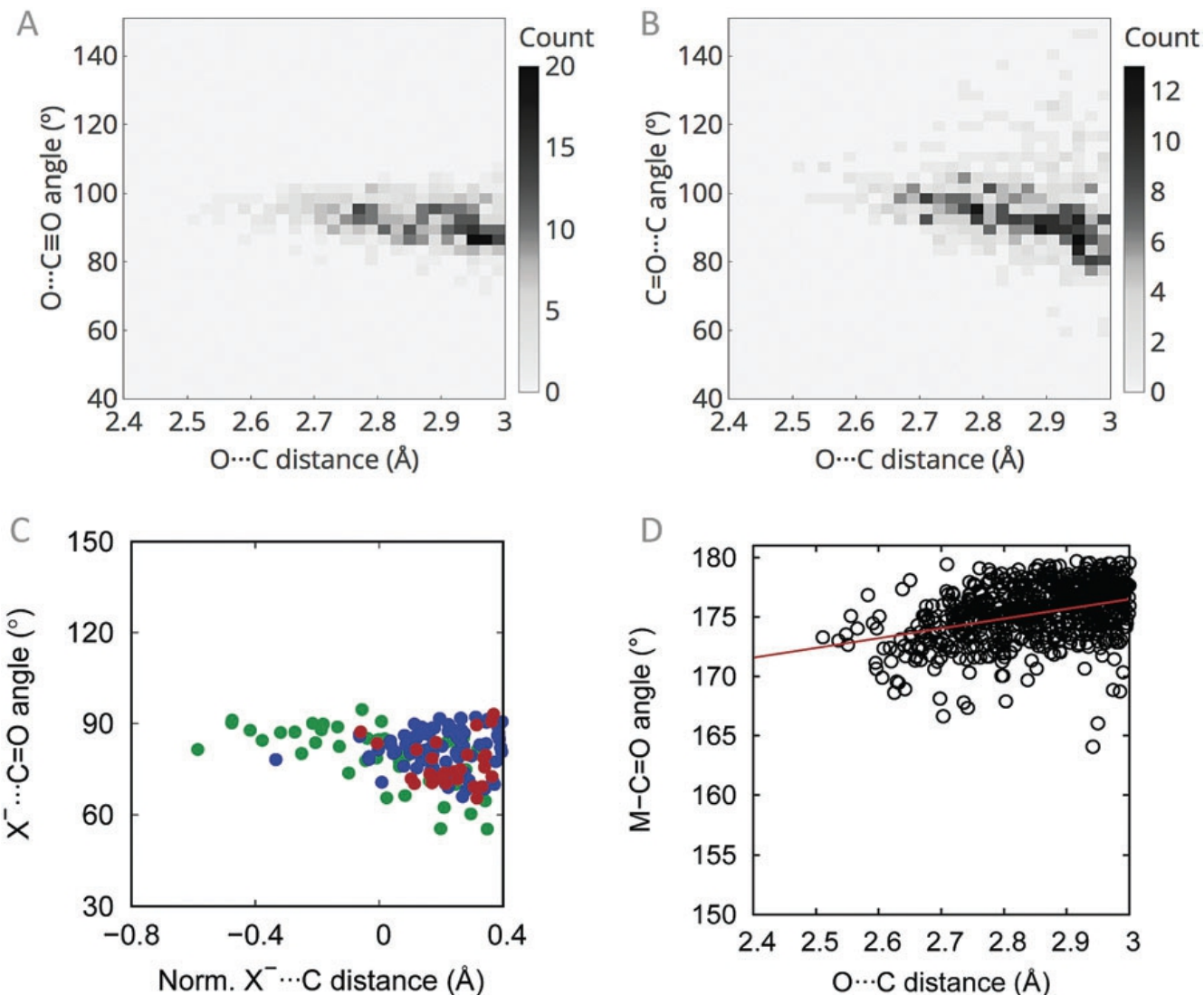
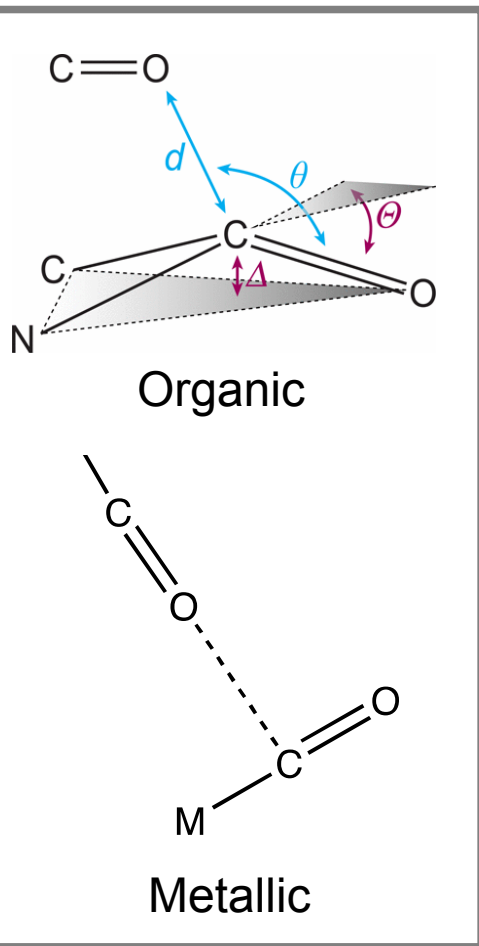
- Dictates protein structure and function

- Present in polymers (PLA), aminoacids and drugs.

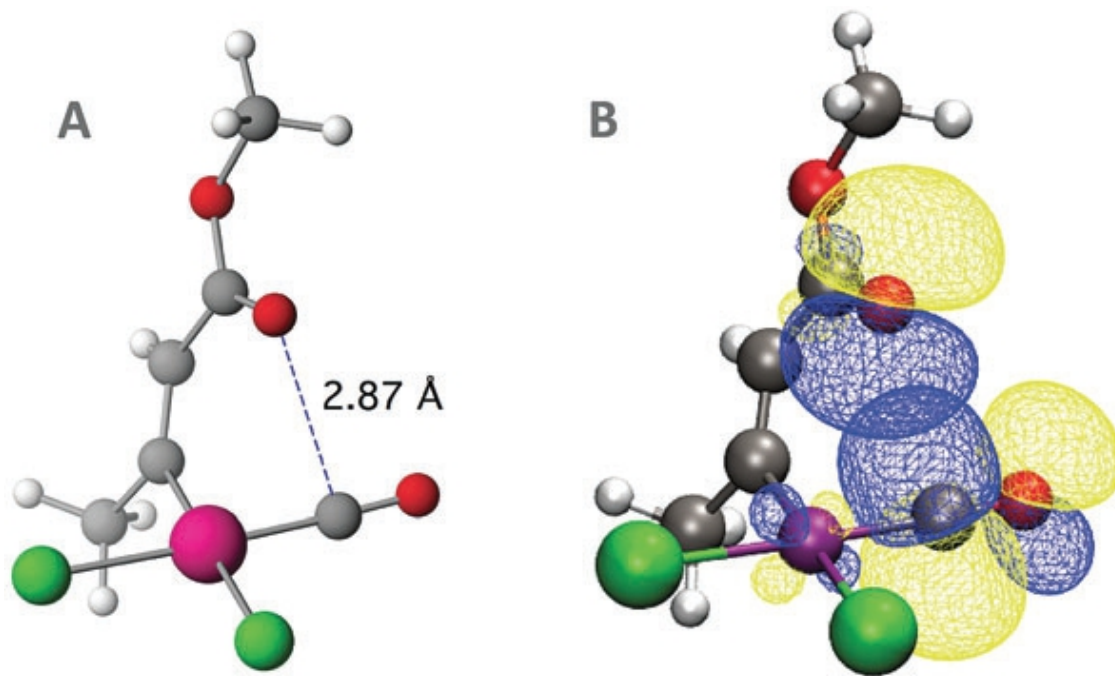
"We anticipate that the $n \rightarrow \pi^$ interaction will be found in an ever-expanding array of molecules, particularly those with a high density of carbonyl groups. Revealing their impact will provoke clever experiments, and interpretation will be guided by computational methodology."*

Newberry and Raines, *Acc. Chem. Res.* **2017**, 50, 1838-1846

The $n \rightarrow \pi^*$ interaction in metal complexes

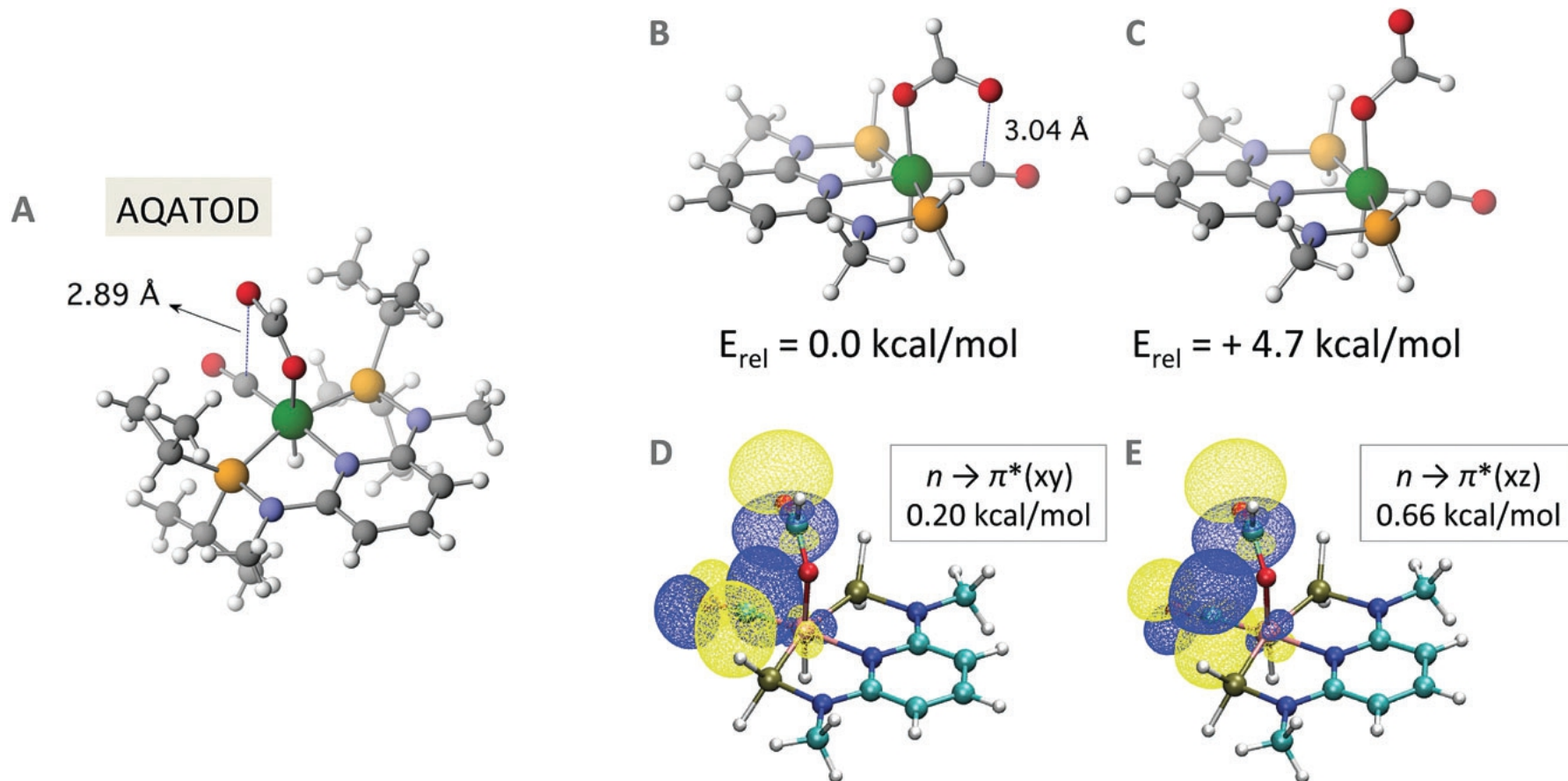


The $n \rightarrow \pi^*$ interaction in metal complexes



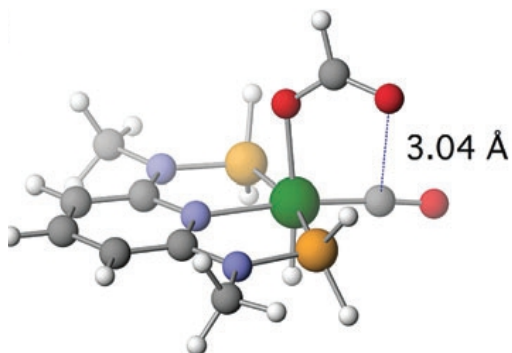
Orbital overlap in a Pt(II) complex

The $n \rightarrow \pi^*$ interaction in metal complexes



The $n \rightarrow \pi^*$ interaction in metal complexes

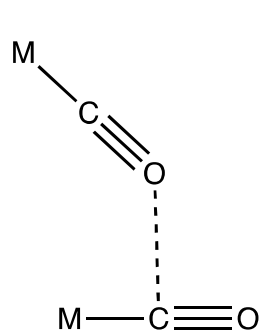
Int. unit	Non-int. unit	Norm. O $\cdots$ C (Å)	O $\cdots$ CO angle (°)	M-CO Angle (°)	E(2) $n \rightarrow \pi^*$ (kcal/mol)
=O	-H	-0.23	104.8	175.4	1.08
=S	-H	-0.12	101.7	171.9	1.79
=O	-CF ₃	-0.19	104.1	175.2	0.87
=O	-CMe ₃	-0.33	103.6	175.0	1.55



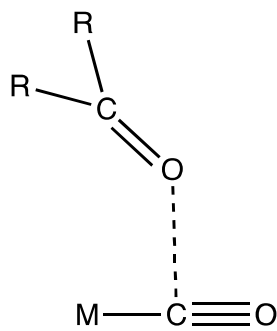
- Sulphur as the donor strengthens the interaction
- All O $\cdots$ CO angles close to the Burgi-Dunitz trajectory
- M-CO angle loses linearity as the interaction makes stronger
- NBO energies larger for good donors (=S, -CMe₃)

The $n \rightarrow \pi^*$ interaction in metal complexes

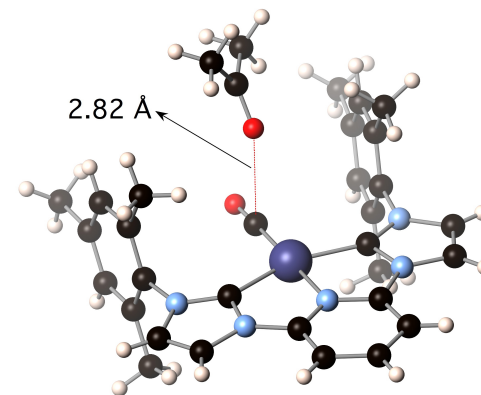
Intermolecular contacts



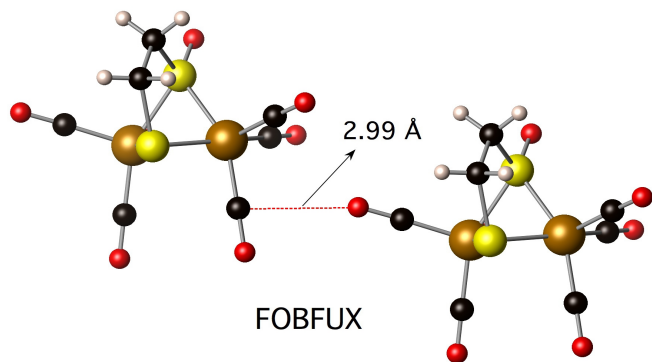
M-CO $\cdots$ CO



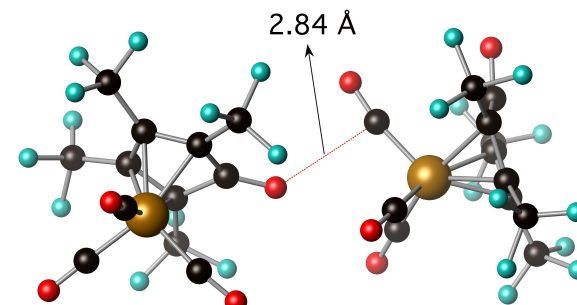
R-CO $\cdots$ CO



BAJNAD



FOBFUX



CFMCFE

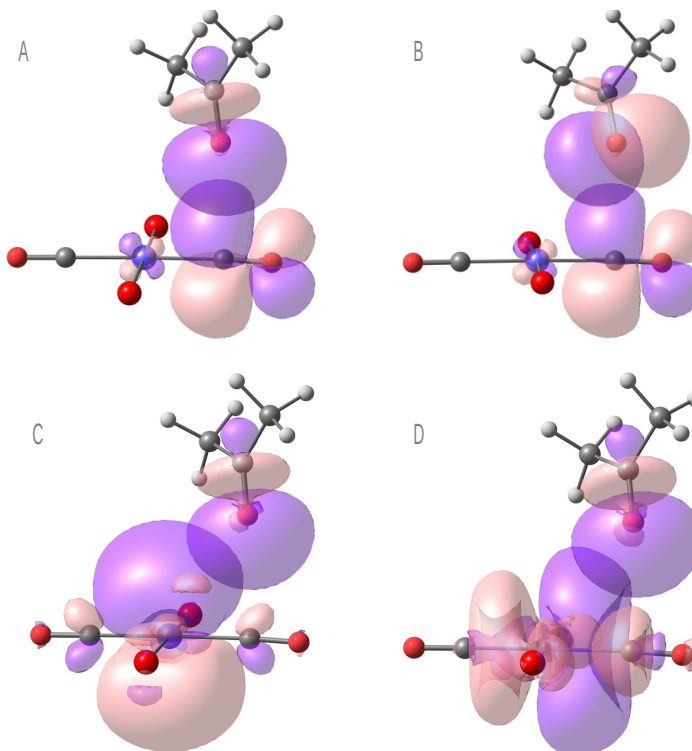
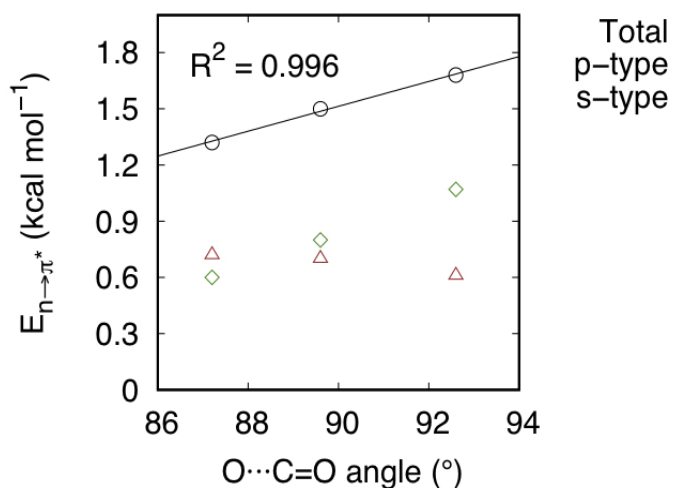
The $n \rightarrow \pi^*$ interaction in metal complexes

Computational study on the nature of the interaction

M	$n(s) \rightarrow \pi_{CO}^*$	$n(p) \rightarrow \pi_{CO}^*$	$n(s) \rightarrow \sigma_{MC}^*$	$n(p) \rightarrow \sigma_{MC}^*$	$n(s) \rightarrow n_M^*$	$n(p) \rightarrow n_M^*$
Ni	1.07	0.61	0.20	0.12	0.22	0.63
Pd	0.80	0.70	0.26	0.16	0.39	0.58
Pt	0.60	0.72	0.87	0.20	1.05	0.62

NBO analysis

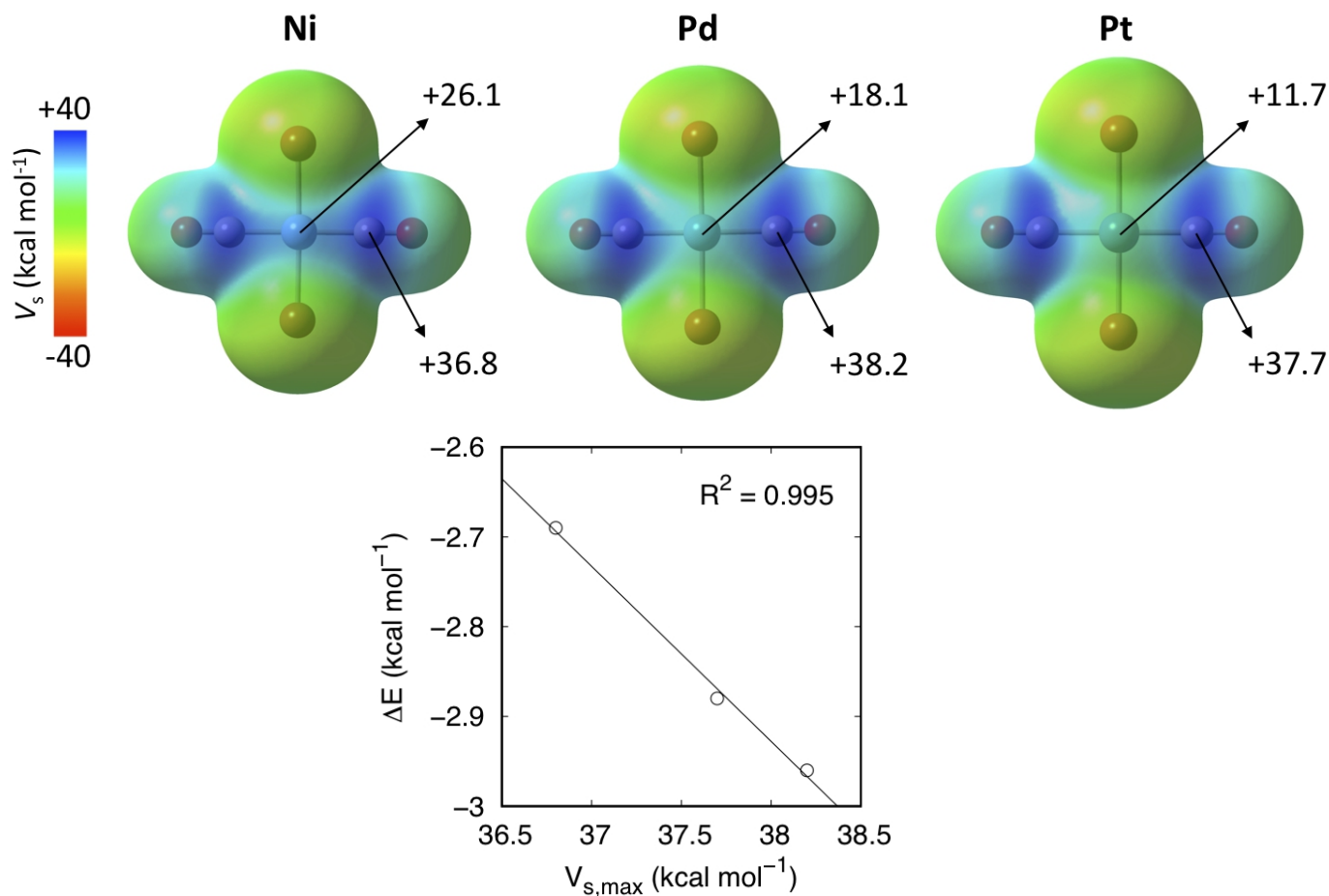
Model system: $[\text{NiBr}_2(\text{CO})_2]$



The $n \rightarrow \pi^*$ interaction in metal complexes

Computational study on the nature of the interaction

MEP analysis



The $n \rightarrow \pi^*$ interaction in metal complexes

Computational study on the nature of the interaction

Energy Decomposition Analysis

Metal	ΔE_{PAULI}	ΔE_{ELECT}	ΔE_{FROZEN}	$\Delta E_{\text{POLARIZ}}$	ΔE_{CT}	ΔE_{INT}
Ni	4.17	-4.86	-0.70 (26)	-0.90 (33)	-1.10 (41)	-2.69
Pd	4.24	-5.19	-0.95 (32)	-0.91 (31)	-1.09 (37)	-2.96
Pt	4.11	-5.11	-1.00 (35)	-0.87 (30)	-1.02 (35)	-2.88

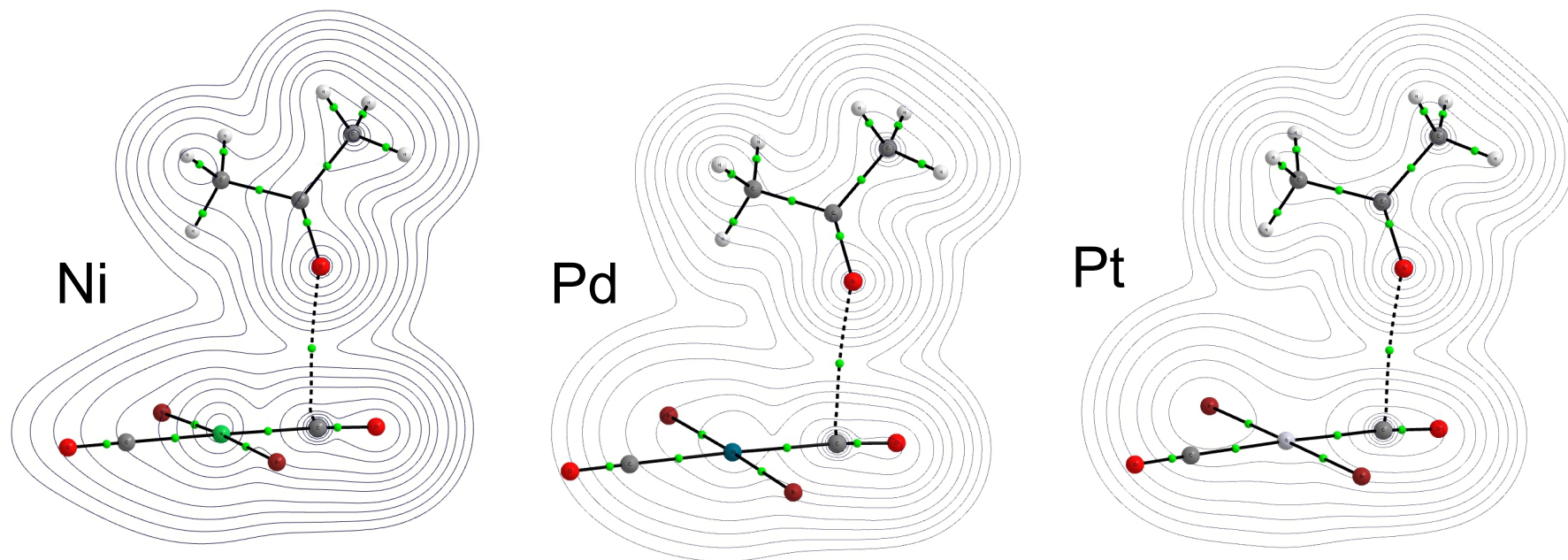
All energies in Kcal/mol

- Electrostatics overcome Pauli repulsion in all cases
- Frozen energy increases when descending the group
- Polarization and Charge Transfer decrease when descending the group

The $n \rightarrow \pi^*$ interaction in metal complexes

Computational study on the nature of the interaction

Atoms in Molecules (AIM) Theory



metal	ρ	$\nabla^2\rho$	$DI(C_{\text{accep}}, O_{\text{donor}})$	H	ϵ
Ni	0.0094	0.0374	0.0422	0.0020	0.7088
Pd	0.0097	0.0382	0.0421	0.0020	0.7710
Pt	0.0094	0.0377	0.0381	0.0020	0.9354

The $n \rightarrow \pi^*$ interaction in metal complexes

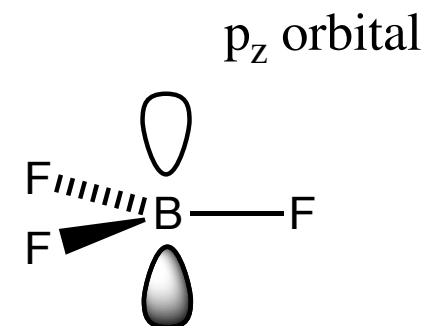
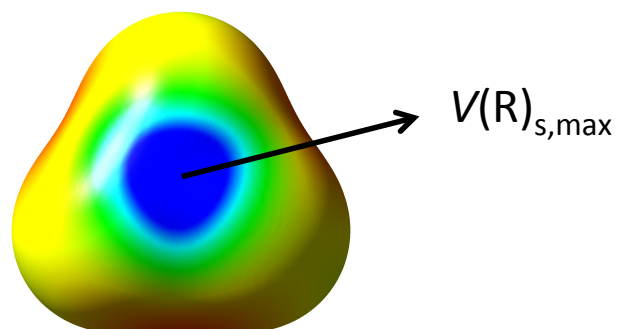
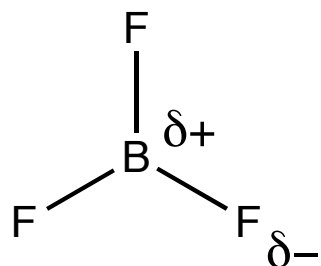
Summary & Conclusions

- Carbonyl...carbonyl contacts, both intra and intermolecular are present in metal complexes.
- These contacts are attractive and follow precise geometrical arrangements.
- The origin of the interaction is the electron delocalization from a lone pair to an antibonding empty orbital.
- Electrostatics can also play an important role in the energy stabilization.
- Opens the way to their use in supramolecular chemistry and crystal design.

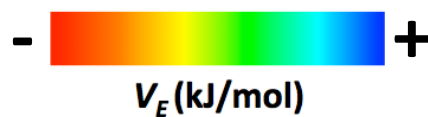
π/σ -hole interactions

The electron density hole concept

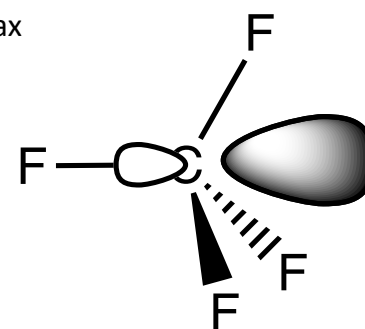
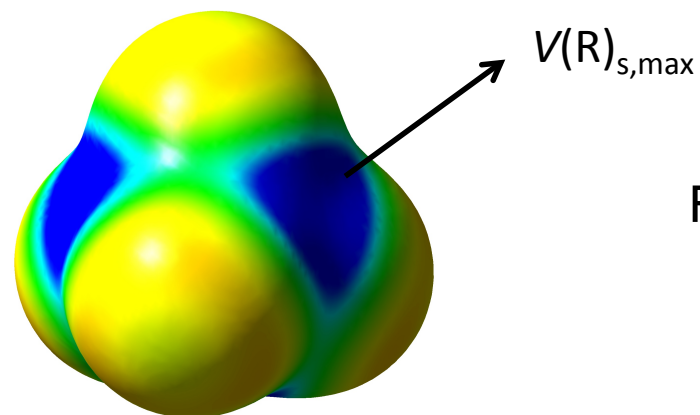
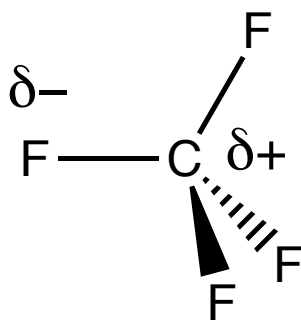
π -hole



MEP

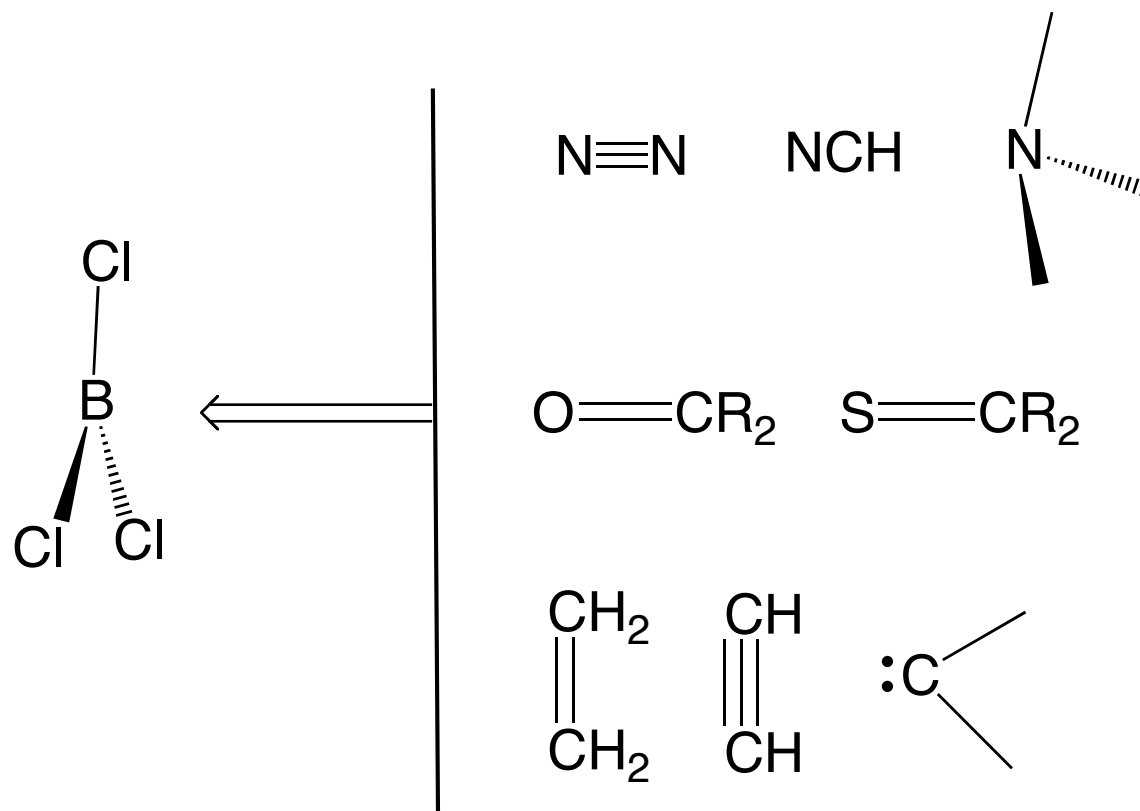


σ -hole



π/σ -hole interactions

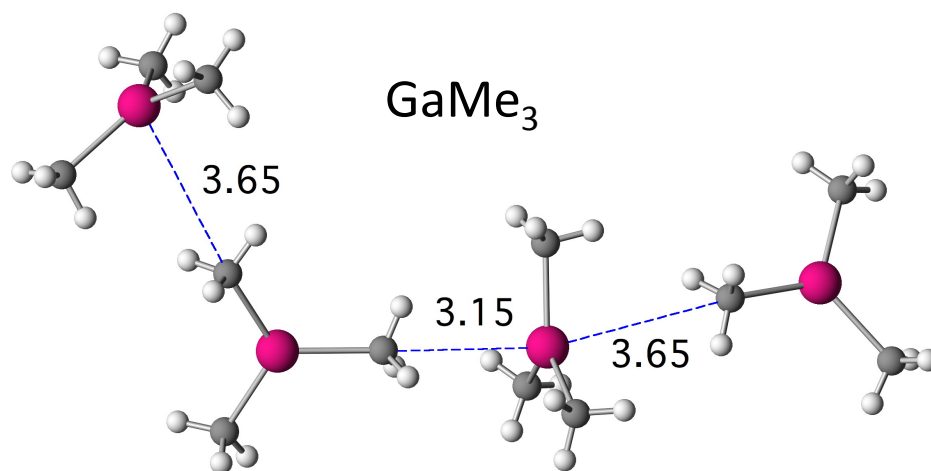
Donors can be: anions, lone pairs, π electron density, carbenes, etc.



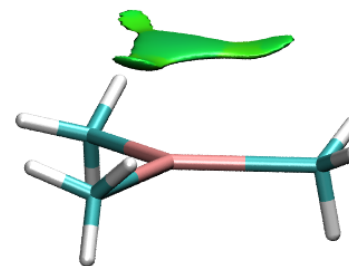
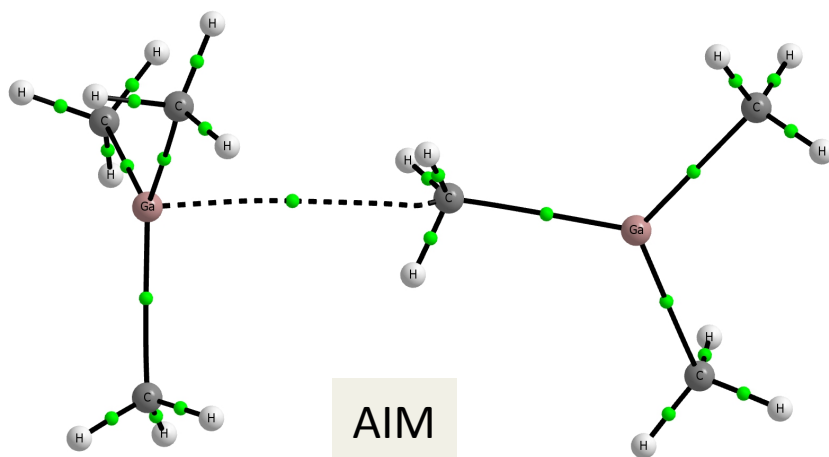
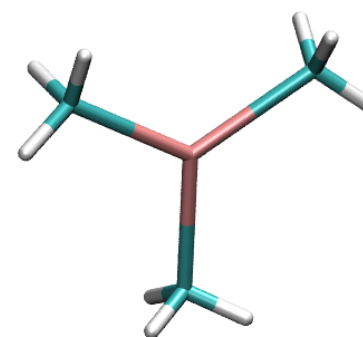
sp^3 carbons?

Alkyl groups as electron density donors

Structural evidence

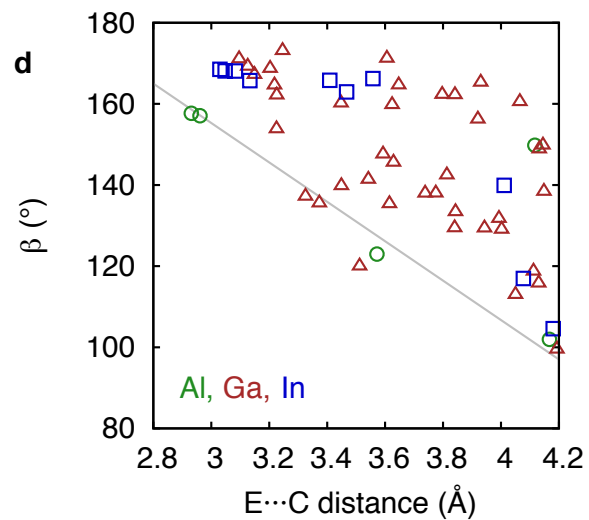
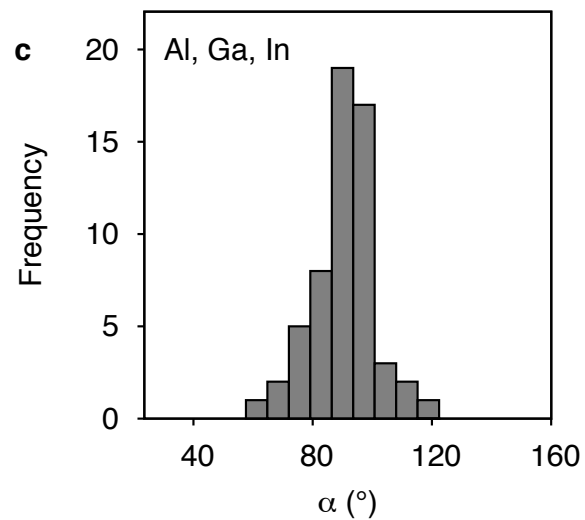
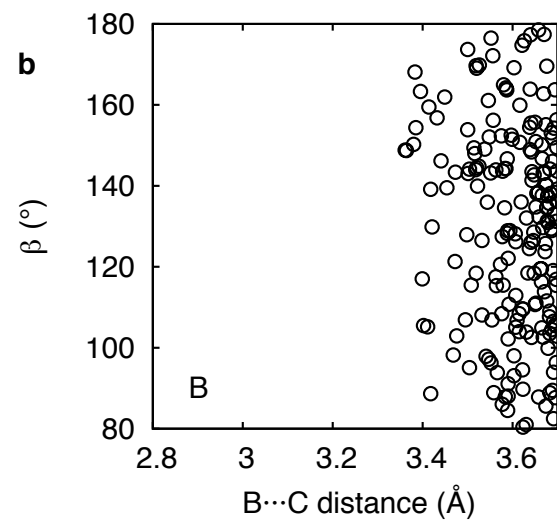
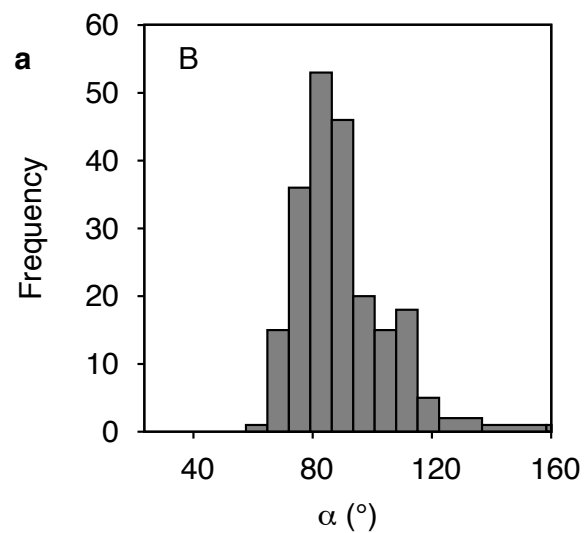
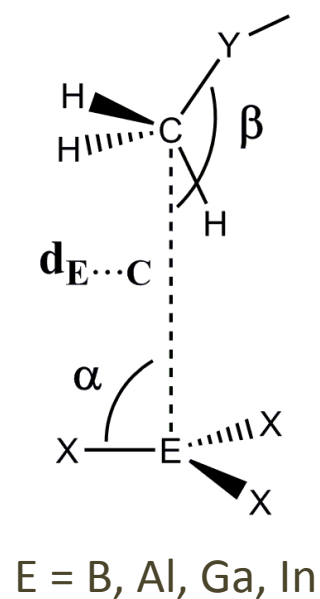


NCIPlot



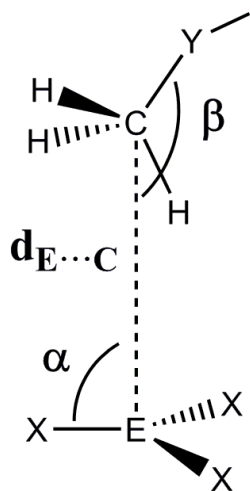
Green areas indicate
weak non-covalent interaction

Alkyl groups as electron density donors

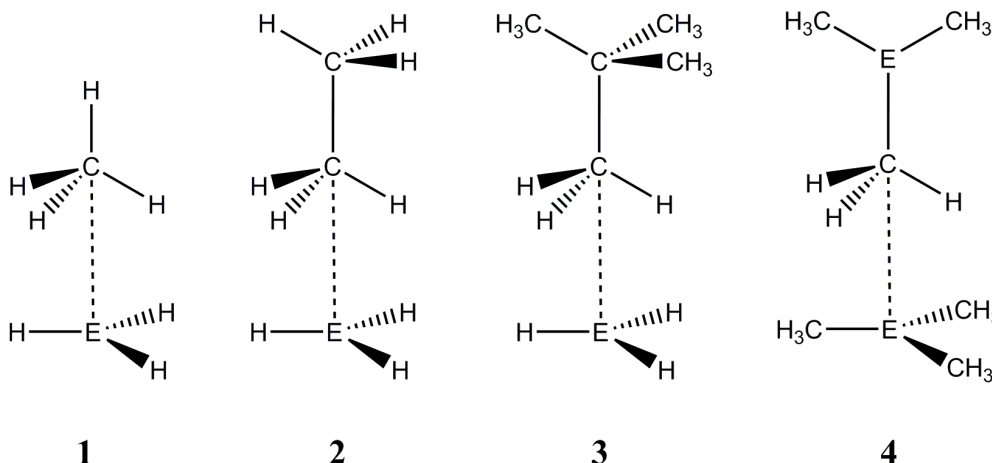


Alkyl groups as electron density donors

Computational analysis (MP2/aug-cc-pVTZ)



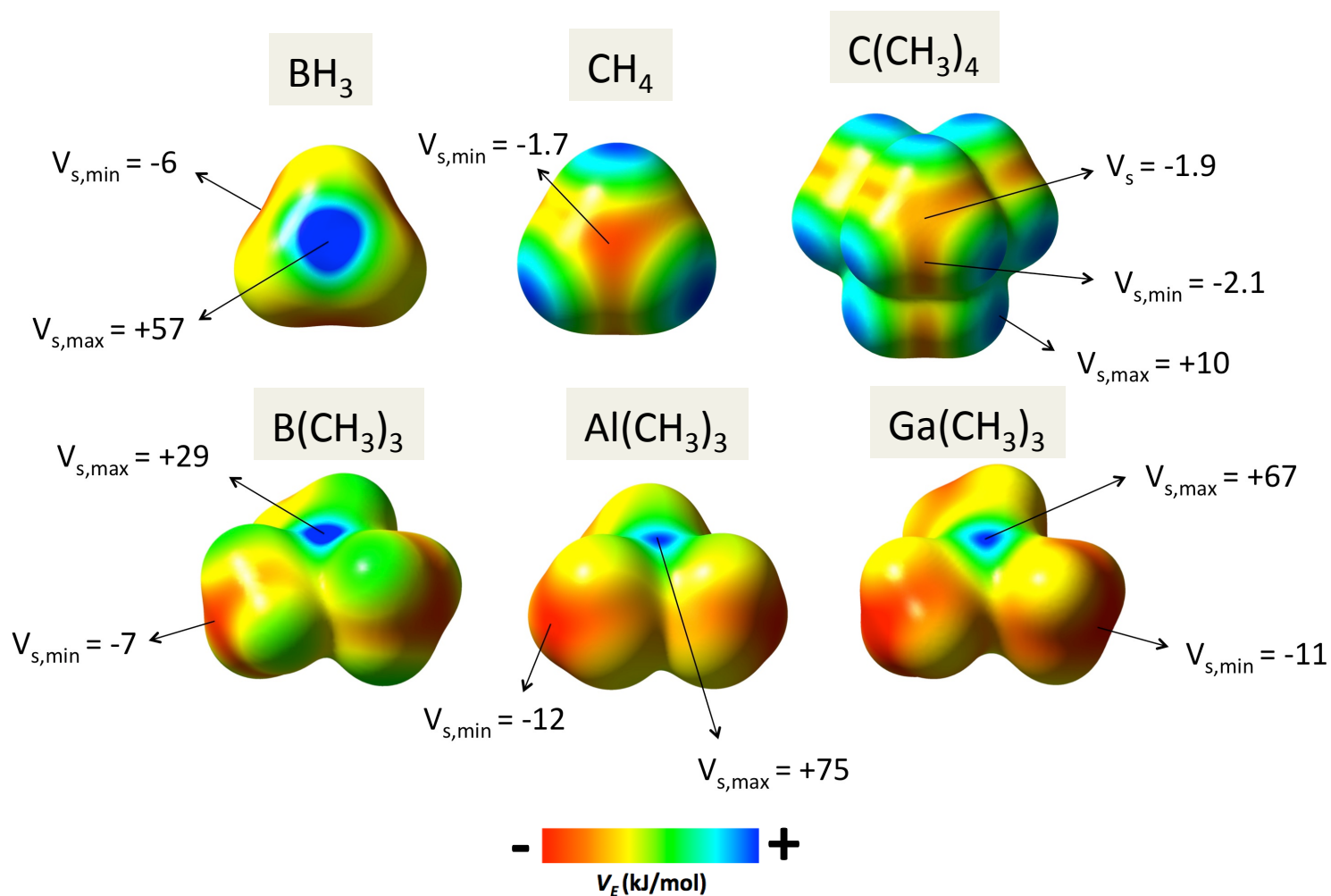
E = B, Al, Ga, In



- Interaction strength: $1 < 2 < 3 < 4$ and $B \ll Ga < Al$
- Angle $\alpha = 90 \pm 5^\circ$
- Angle β : for Al and Ga $\approx 140 - 180^\circ$
- Good match with experimental structures

Alkyl groups as electron density donors

Nature of the interaction



- Good agreement with Interaction strength: **B** << **Ga** < **Al**

Alkyl groups as electron density donors

Nature of the interaction

ENERGY DECOMPOSITION ANALYSIS (kcal/mol) [B3LYP-D3]

Dimer	ΔE_{Pauli}	ΔE_{Elec}	ΔE_{Disp}	ΔE_{Pol}	ΔE_{CT}	ΔE_{int}
$[\text{B}(\text{CH}_3)_3]_2$	6.53	-4.18	-3.63	-0.14	-0.51	-1.94
$[\text{Al}(\text{CH}_3)_3]_2$	25.44	-16.46	-5.14	-6.44	-3.83	-6.45
$[\text{Ga}(\text{CH}_3)_3]_2$	27.75	-16.71	-5.58	-5.45	-3.49	-3.32

- Electrostatic: The largest term in all cases ($\approx 50\%$)
- Dispersion: For B is 43%, for Al and Ga only 16 - 17%
- Orbital: Significant for Al and Ga; negligible for B

The silane-methane dimer



Available online at www.sciencedirect.com

SCIENCE @ DIRECT®

Chemical Physics Letters 397 (2004) 314–318

CHEMICAL
PHYSICS
LETTERS

www.elsevier.com/locate/cplett

A theoretical study of the dispersion-bound silane–methane dimer

E.R. Johnson, G.A. DiLabio *

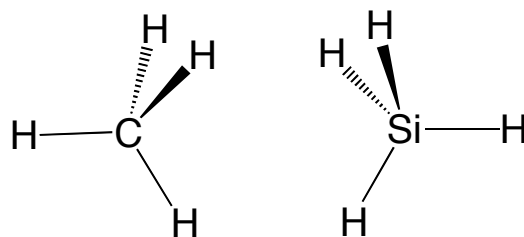
*National Institute for Nanotechnology, National Research Council of Canada, W6-010 ECERF, 9107-116th Street, Edmonton,
Alberta, Canada T6G 2V4*

Received 29 July 2004; in final form 26 August 2004
Available online 16 September 2004

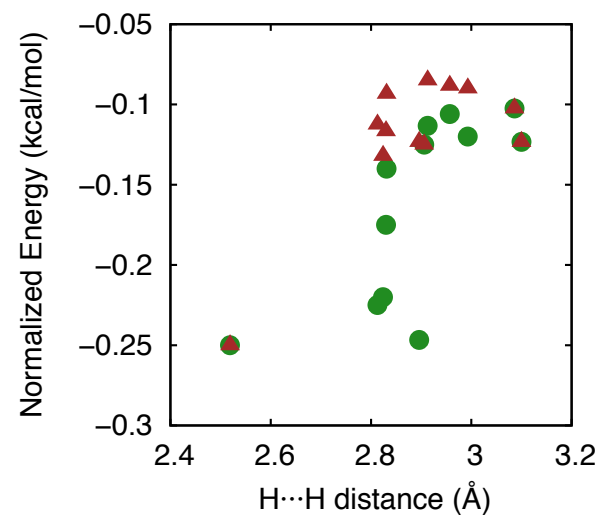
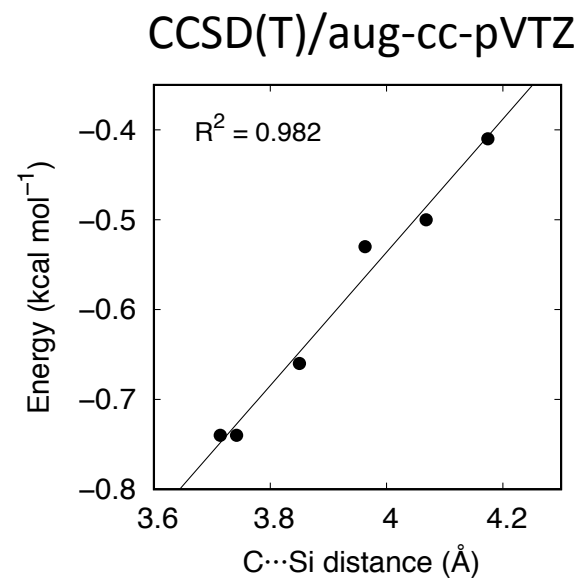
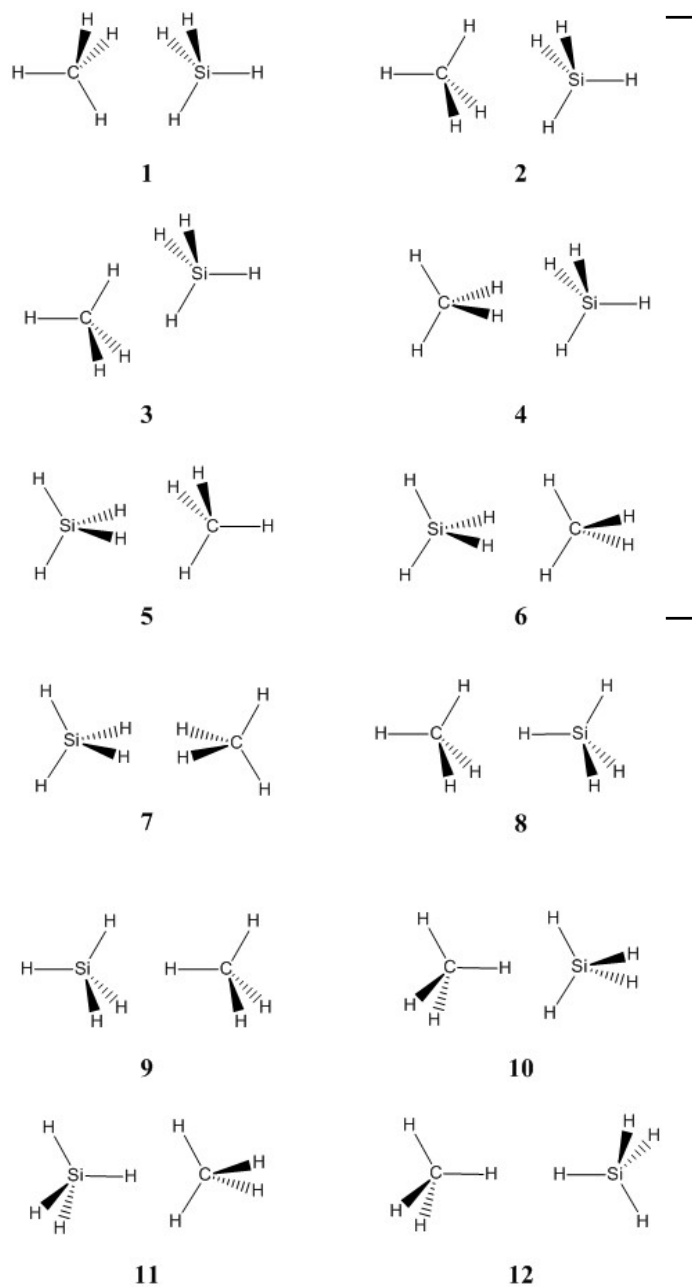
Abstract

We studied six conformers of the silane–methane dimer using CCSD(T) with basis sets up to aug-cc-pVQZ. The binding energies of the conformers increase with the number of hydrogen contacts between the monomers. The most stable conformer has an eclipsed, C_{3v} arrangement and is bound by 0.81 kcal/mol. The use of counterpoise corrections and basis set extrapolation schemes separately give unsatisfactory binding energies. However, extrapolation of the counterpoise corrected energies provided binding energies in excellent agreement with counterpoise-corrected CCSD(T)/aug-cc-pVQZ results.

© 2004 Elsevier B.V. All rights reserved.

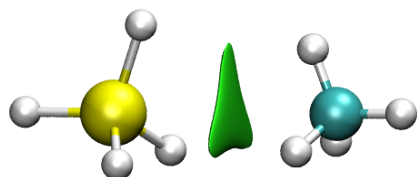


The silane-methane dimer revisited

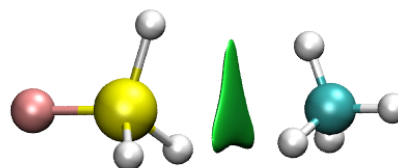


The silane-methane dimer revisited

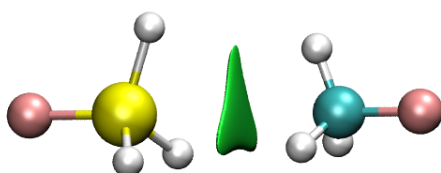
NCIPlot surfaces



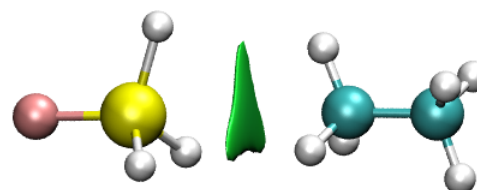
-0.74 kcal/mol



-1.00 kcal/mol



-0.12 kcal/mol



-1.16 kcal/mol

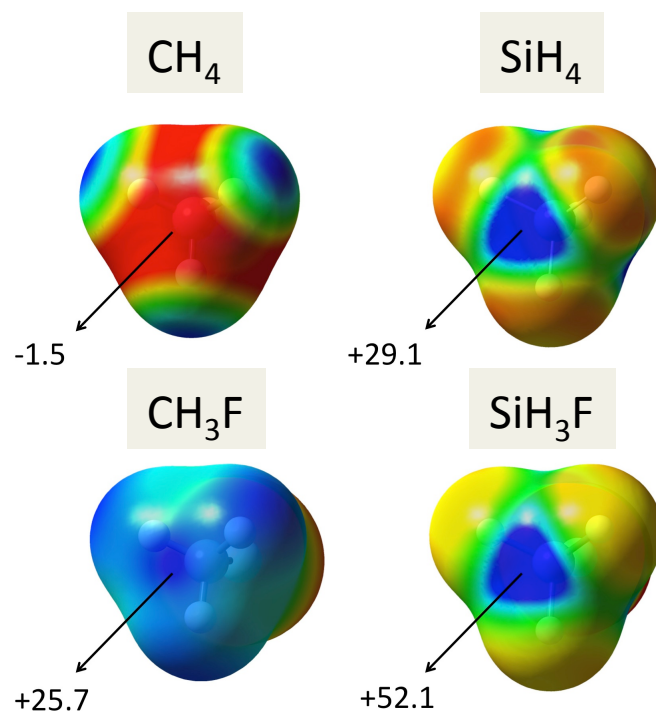
σ -donors in C / σ -attractors in Si



Strengthen the interaction

Electrostatic interaction?

The silane-methane dimer revisited



ALMO-EDA (B3LYP-D3) kcal/mol

Dimer	Topol.	ΔE_{Pauli}	ΔE_{Elec}	ΔE_{Disp}	ΔE_{Pol}	ΔE_{CT}	ΔE_{int}
$\text{CH}_4 \cdots \text{SiH}_4$	1	2.381	-1.51 (48)	-1.37 (44)	-0.04 (1)	-0.20 (7)	-0.74
$\text{FCH}_3 \cdots \text{SiH}_4$	1	2.034	-1.02 (38)	-1.36 (51)	-0.09 (3)	-0.18 (7)	-0.61
$\text{FCH}_3 \cdots \text{SiH}_3\text{F}$	1	2.096	-0.58 (25)	-1.43 (61)	-0.14 (6)	-0.18 (8)	-0.23
$\text{H}_3\text{C}-\text{CH}_3 \cdots \text{SiH}_3\text{F}$	1	3.558	-2.39 (51)	-1.80 (38)	-0.16 (3)	-0.37 (8)	-1.18
$\text{CH}_4 \cdots \text{SiH}_4$	12	0.953	-0.58 (47)	-0.49 (40)	-0.01 (1)	-0.14 (12)	-0.27

Summary

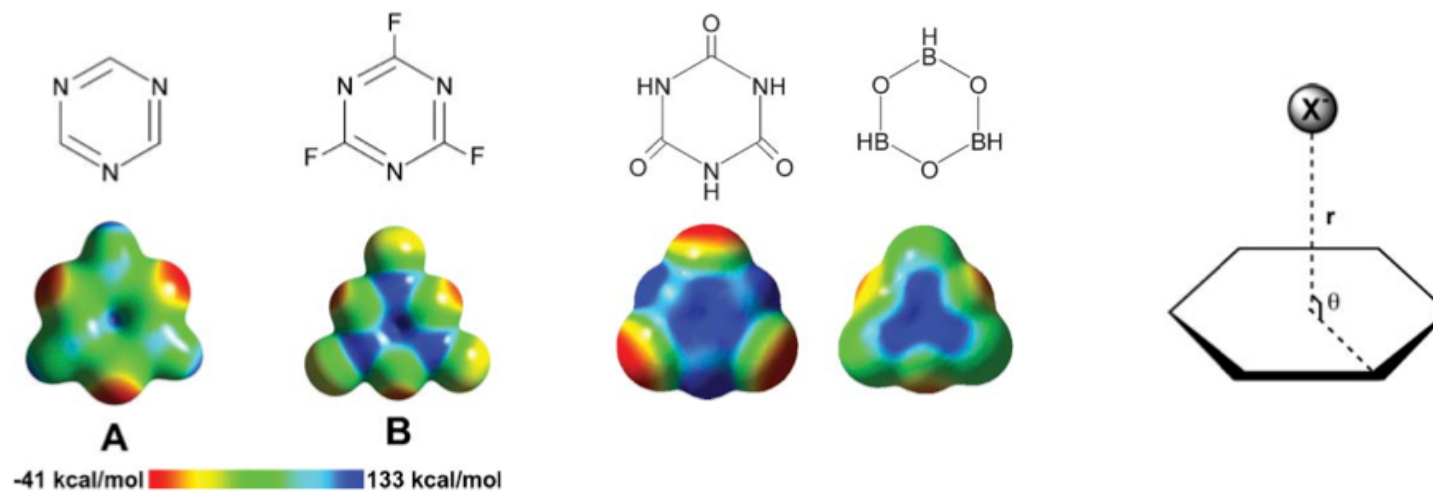
- Alkyl groups can act as donors in π - and σ -hole bonding
- Structural evidence of interaction with triel Lewis acids
- Directional and relatively strong interaction (1 – 8 kcal/mol)
- Electrostatic nature with significant orbital contribution for Al and Ga
- Electrostatics / dispersion interplay dominates methane-silane
- Interaction strength can be modulated by substitution

J. Echeverría, [*CrystEngComm*](#) **2017**, *19*, 6289 - 6296

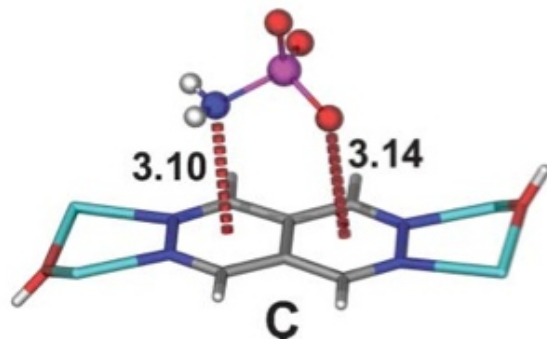
J. Echeverría, [*Phys. Chem. Chem. Phys.*](#) **2017**, *19*, 32662 - 32669

Anion- π interactions

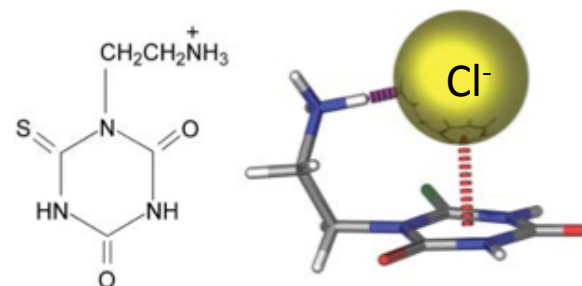
Electron depleted rings



Anion- π

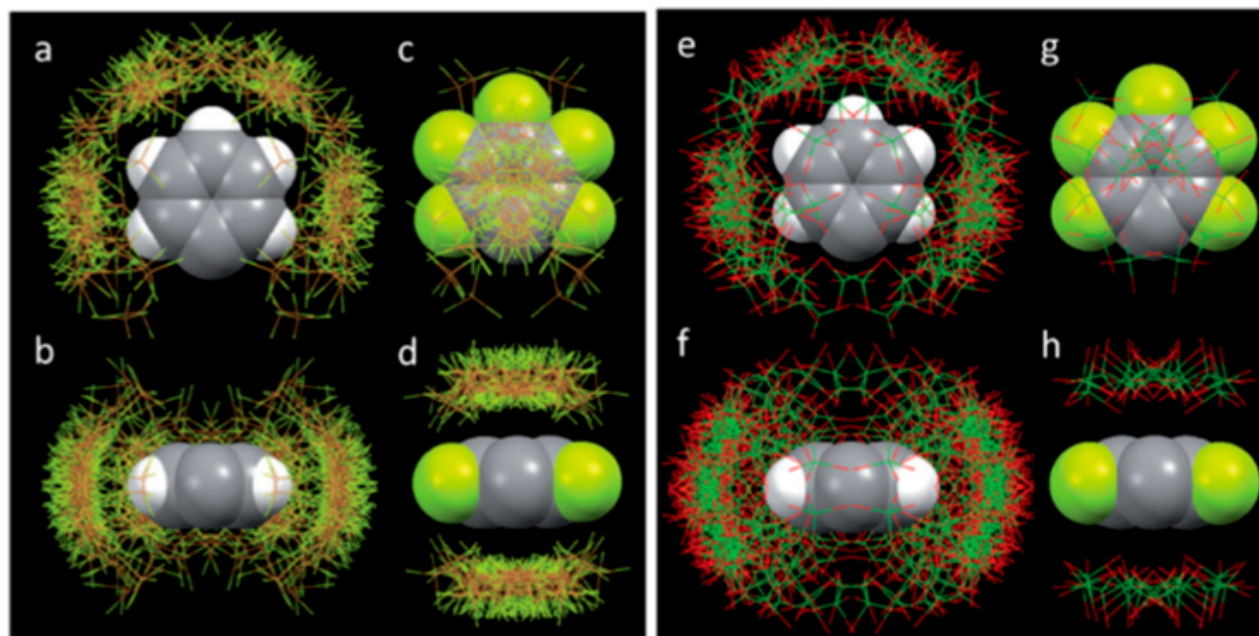


Anion- π + H-bond



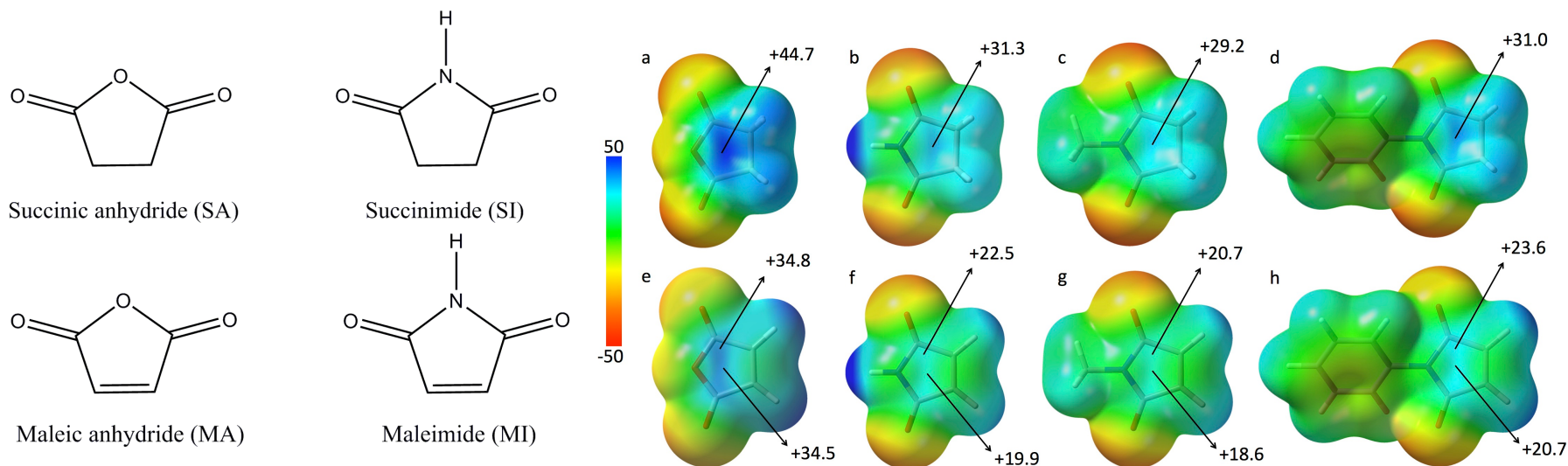
Anion- π interactions

IsoStar plots of contacts between C_6H_6 / C_6F_6 and BF_4^- and ClO_4^-

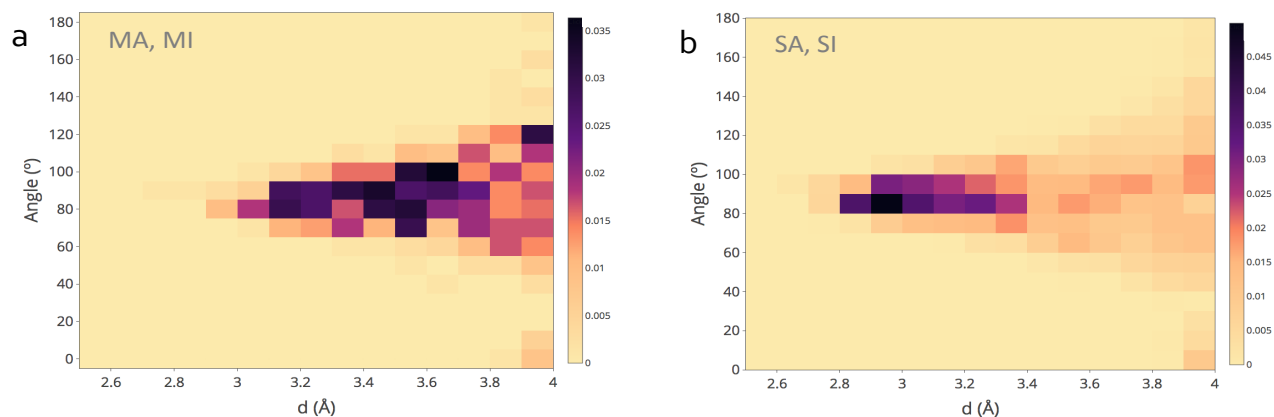
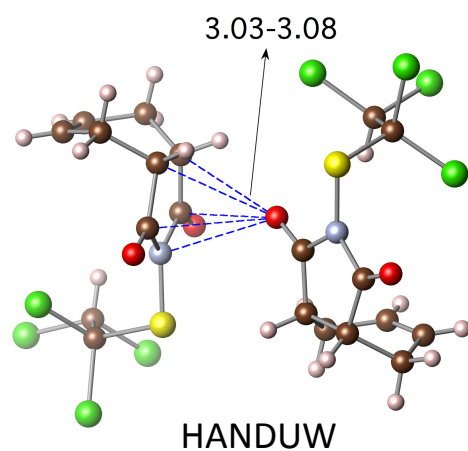


Lone pair- π interactions

Noncovalent interactions in succinic and maleic anhydride derivatives



CSD Structural Analysis



Take Home Message

- NCIs are everywhere, they are subtle but not faint
- Important when working additively or cooperatively
- They can affect properties of materials, crystal packing, surface adsorption, etc.
- Structural databases are key to see trends
- In calculations, look for trends to rationalize

Acknowledgements



Dr. Gabriel Aullón



Prof. Santiago Alvarez



IQTC-UB and CSUC for computational facilities